

2015 Revised Basic Math
Answer Key

Explanation of diagonal movement and an example:

$$5X = 20$$

Question #1 regarding Example #1: Is the **X** in the numerator? **YES**

Question #2 regarding Example #1: Is the **X** alone on one side of the equation? **NO**

How do we use diagonal movement to place **X** alone on one side of the equation?

Answer:

- Divide both sides by "5" to get **X** alone and **treat both sides of the equation equally**. Notice that the 5 was moved from the top of the left side to the bottom of the right side of the equation – **a diagonal move**.

$$\frac{5X}{5} = \frac{20}{5}$$

FINAL ANSWER: $20 \div 5 = 4$

ANSWER KEY: 2017 Revised Basic Math
February 2017

Practice Problem: Steps to solving problems using unit cancellation

Practice Problem: How many minutes are there in a day?

Problem Set Up

List all known and unknown data.

Unknown: ? $\frac{\text{min}}{\text{day}}$	Known: 60 $\frac{\text{mins}}{\text{hr}}$	24 $\frac{\text{hrs}}{1}$
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Step 1: List unknown data including units in vertical format followed by an equal sign.

$$\frac{? \text{ min}}{\text{day}} =$$

Step 2: Find data (known or a conversion) that has the same numerator unit as the unknown numerator. Place it to the right of the equal sign. Add a multiplication sign.

Positions your numerator unit

$$\frac{? \text{ min}}{\text{day}} = 60 \frac{\text{min}}{1 \text{ hr}} \times$$

Steps 3 and 4: To cancel unwanted denominator unit, find data (known or a conversion) that has the same numerator unit. Place it to the right of data used in Step 2. Place a multiplication sign between each piece of data. Continue to place data (known or a conversion) into equation to systematically cancel all unwanted units until only the unknown denominator units remain.

Cancel unwanted units that match

$$\frac{? \text{ min}}{\text{day}} = 60 \frac{\text{min}}{1 \text{ hr}} \times 24 \frac{\text{hrs}}{1 \text{ day}}$$

Step 5: Multiply the values of all numerators and place this value in the numerator of the answer. Multiply the values of all denominators and place this value in the denominator of the answer. Divide to calculate the final answer.

$$\frac{? \text{ min}}{\text{day}} = 60 \frac{\text{min}}{1 \text{ hr}} \times 24 \frac{\text{hrs}}{1 \text{ day}} = 1440 \frac{\text{min}}{1 \text{ day}}$$

These are the correct units in both numerator and denominator

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

Pressure/Height Conversions

Practice Problem calculating psi: The water level at the top of a fully filled water standpipe is 150 feet above the elevation of a water tap. The tank contains 50,000 gallons of water. What is the approximate pressure at the tap?

$$? \text{ psi} = \frac{1 \text{ psi}}{2.31 \text{ ft}} \times 150 \text{ ft} = \frac{150 \text{ psi}}{2.31} = \mathbf{64.9 \text{ psi}}$$

Note: Remember pressure is not affected by volume, only **height**.

Practice Problem calculating height in ft: An elevated tank records a pressure of 25 psi, what is the height of water in the tank?

To calculate **height in ft** from psi:

$$? \text{ ft} = \frac{2.31 \text{ ft}}{1 \text{ psi}} \times 25 \text{ psi} = \mathbf{58 \text{ ft}}$$

Temperature Conversions

Practice Problem Solving for °C: Convert 60°F into °C

$$^{\circ}\text{C} = \frac{^{\circ}\text{F} - 32}{1.8} \quad 60 - 32 = \mathbf{28} = \mathbf{15.5^{\circ}\text{C}}$$

Practice Problem Solving for °F: Convert 20°C into °F

$$^{\circ}\text{F} = (^{\circ}\text{C} \times 1.8) + 32$$

$$^{\circ}\text{F} = 20 \times 1.8 = 36 + 32 = \mathbf{68^{\circ}\text{F}}$$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

Unaccounted Water Calculation

Practice Problem: In one month a water system produced 5,500,000 gallons of water. Of the total water, 4,500,000 gallons were billed, 250,000 were used for fire protection and 200,000 gallons were used for flushing. What is the total unaccounted for water loss percentage for this month?

Step 1: Add total gallons accounted for (billed, fire protection and flushing)

Gallons Accounted for = **4,500,000** (billed) + **250,000** (fire protection) + **200,000** (flushing) = **4,950,000**

Step 2: Subtract “accounted for” from total produced to find “Unaccounted for”

5,500,000 – **4,950,000** (Step 1 Accounted for) = **550,000** (Unaccounted for)

Step 3: Divide “Unaccounted for” by total produced and multiply by 100 to equal the % unaccounted for

550,000 (Step 2 Unaccounted For) = **0.1** X 100 = **10** % Unaccounted for
5,500,000 (Total Produced)

Area of a Rectangle

Practice Problem: The sedimentation basin for the filtration plant is 25 ft. x 15 ft. What is the area in square feet?

Area = (L) X (W) = 25 ft. X 15 ft. = **375** ft²

Area of a Rectangle – Converting inches to feet

Practice Problem: The filter unit at the plant is 15 ft. 6 inches long, and 15ft. 6 inches wide. What is the area of the filter?

Step 1: Convert inches to feet

The first step in solving this problem is to change the inch units to feet units. The tank is 15 feet. 6 inches long, by 15 feet 6 inches wide.

$$? \text{ ft} = 1 \frac{\text{ft}}{12 \text{ inches}} \times 6 \text{ inches} = \frac{6}{12} = \mathbf{0.5 \text{ ft}}$$

Step 2: Add 0.5 ft to the length and the width and insert into equation and multiply L X W.

$$\text{Area} = (L) \times (W) = 15.5 \text{ ft} \times 15.5 \text{ ft} = \mathbf{240.25 \text{ ft}^2}$$

Area of a Circle

Practice Problem: The day tank for the coagulant is 4 feet in diameter, what is the area in square feet?

$$\text{Area} = (0.785)(\text{Diameter})^2 = (0.785)(4 \text{ ft})(4 \text{ ft}) = \mathbf{12.56 \text{ ft}^2}$$

Area of a Circle – Converting inches to feet

Practice Problem: The chemical feed tank is 20 inches in diameter, what is the area of the chemical feed tank?

Step 1: Convert inches to feet

$$? \text{ ft} = 1 \frac{\text{ft}}{12 \text{ inches}} \times 20 \text{ inches} = \mathbf{1.67 \text{ ft}}$$

Step 2: Insert diameter (in ft) into area formula and do the math.

$$\text{Area} = (0.785)(D)^2 = (0.785)(1.67 \text{ ft})(1.67 \text{ ft}) = \mathbf{2.19 \text{ ft}^2}$$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

Volume of a Rectangle in ft³

The formula for volume of a rectangle is length X width X height or depth, or (L)(W)(H or D)

Note: For this equation, the terms “height” and “depth” are interchangeable.

Practice Problem: What is the volume of a clearwell that is 40 feet long, by 40 feet wide, by 12 feet deep?

$$V = (L)(W)(D) = (40 \text{ ft})(40 \text{ ft})(12 \text{ ft}) = \mathbf{19,200 \text{ ft}^3}$$

Volume of a Circular Tank in ft³

Example Problem: What is the volume in cubic feet of a tank that is 22 feet in diameter, and filled to 8 feet deep?

$$V = 0.785(\text{Dia})^2(\text{H})$$

$$V = 0.785(22 \text{ ft})(22 \text{ ft})(8 \text{ ft})$$

$$V = \mathbf{3039.5 \text{ ft}^3 \text{ or } 3040 \text{ ft}^3}$$

Volume of a Circular Tank in ft³ – Converting inches to feet

Practice Problem: What is the volume of a day tank that is filled to 3 feet, and is 20 inches wide?

Step 1: Convert inches to feet

$$? \text{ ft} = \frac{1 \text{ ft}}{12 \text{ inches}} \times 20 \text{ inches} = \mathbf{1.67 \text{ ft}}$$

Step 2: Insert diameter (in ft) into volume formula and do the math.

$$V = 0.785(1.67 \text{ ft})(1.67 \text{ ft})(3 \text{ ft}) = \mathbf{6.6 \text{ ft}^3}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

Volume of a Rectangular Tank – Converting ft³ to gallons

The problems in the previous examples requested the volume measured in units of cubic feet. More often, the volumes are measured in gallons. The conversion factor to go from cubic feet to gallons is:

$$1 \text{ ft}^3 = 7.48 \text{ gallons}$$

To convert ft³ to gallons, use this equation:

$$\text{Gallons} = \text{volume in ft}^3 \times 7.48$$

$$\begin{array}{l} 1 \text{ ft}^3 \\ 7.48 \text{ gallons} \end{array}$$

Therefore, if we were asked to calculate the volumes in the previous problems in gallons instead of cubic feet, the solution would require one extra step.

Practice Problem: What is the volume, in **gallons**, of a tank 40 feet square and filled to 12 feet deep?

Step 1: Solve the volume equation in ft³:

$$V = (L)(W)(D) = (40 \text{ ft})(40 \text{ ft})(12 \text{ ft}) = \mathbf{19,200 \text{ ft}^3}$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = 7.48 \frac{\text{gal}}{1 \text{ ft}^3} \times \mathbf{19,200 \text{ ft}^3} = \mathbf{143,616 \text{ gallons}}$$

Volume of a Circular Tank – Converting ft³ to gallons

Practice Problem: What is the volume, in gallons, of a day tank that is filled to 3 feet, and is 20 inches wide?

Step 1: Convert inches to feet

$$? \text{ ft} = 1 \frac{\text{ft}}{12 \text{ inches}} \times 20 \text{ inches} = \underline{1.67} \text{ ft}$$

Step 2: Insert diameter (in ft) into volume formula and do the math.

$$V = 0.785(1.67 \text{ ft})(1.67 \text{ ft})(3 \text{ ft}) = \underline{6.6} \text{ ft}^3$$

Step 3: Convert ft³ into gallons:

$$? \text{ gal} = 7.48 \frac{\text{gal}}{1 \text{ ft}^3} \times \underline{6.6} \text{ ft}^3 = \underline{49.3} \text{ gallons}$$

QUIZ # 1

1. What is the **volume in ft³**, of a sedimentation basin that is 22 feet long, and 15 feet wide, and filled to 10 feet?

$$V = (L)(W)(H) = (22\text{ft})(15\text{ft})(10\text{ft}) = \underline{3300} \text{ ft}^3$$

2. What is the **volume in gallons** of a clear well that is 35 feet long, 30 feet wide, and filled to 18 feet?

Step 1: Solve the volume equation in ft³

$$V = (L)(W)(D) = (35 \text{ ft})(30 \text{ ft})(18 \text{ ft}) = \underline{18900} \text{ ft}^3$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = 7.48 \frac{\text{gal}}{1 \text{ ft}^3} \times \underline{18900} \text{ ft}^3 = \underline{141,372} \text{ gallons}$$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

3. What is the **volume in gallons** of a storage tank that is 20 feet in diameter, and filled to 18 feet?

Step 1: Solve the volume equation in ft³:

$$V = 0.785(\text{Dia})^2(H)$$

$$V = 0.785(20 \text{ ft})(20 \text{ ft})(18 \text{ ft}) = \underline{5652 \text{ ft}^3}$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = \frac{7.48 \text{ gal}}{1 \text{ ft}^3} \times \underline{5652 \text{ ft}^3} = \underline{42,277} \text{ gallons (rounded)}$$

4. What is the **volume in gallons** of a clear well that is 40 feet 8 inches square, and filled to 12 feet deep?

Step 1: Convert inches to feet

$$? \text{ ft} = \frac{1 \text{ ft}}{12 \text{ inches}} \times 8 \text{ inches} = \underline{0.67 \text{ ft}}$$

Step 2: Insert diameter (in ft) into volume formula and do the math.

$$V = (L)(W)(D) = (40.67 \text{ ft})(40.67 \text{ ft})(12 \text{ ft}) = \underline{19848.5 \text{ ft}^3}$$

Step 3: Convert ft³ into gallons:

$$? \text{ gal} = \frac{7.48 \text{ gal}}{1 \text{ ft}^3} \times \underline{19848.5 \text{ ft}^3} = \underline{148,467} \text{ gallons}$$

5. What is the **volume in ft³** of an elevated clear well that is 17.5 feet in diameter, and filled to 14 feet?

$$\text{Volume (ft}^3) = (0.785)(D)^2(h) =$$

$$V = (0.785)(17.5\text{ft})(17.5\text{ft})(14\text{ft}) = \underline{3,366 \text{ ft}^3}$$

6. What is the **pressure (psi)** at the bottom of an elevated tank filled to 60 feet of water?

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

$$? \text{ psi} = \frac{1 \text{ psi}}{2.31 \text{ ft}} \times 60 \text{ ft} = \frac{60 \text{ psi}}{2.31} = \mathbf{26 \text{ psi}}$$

7. Convert 80 ° F to °C.

$$^{\circ}\text{C} = \frac{^{\circ}\text{F}-32}{1.8}$$

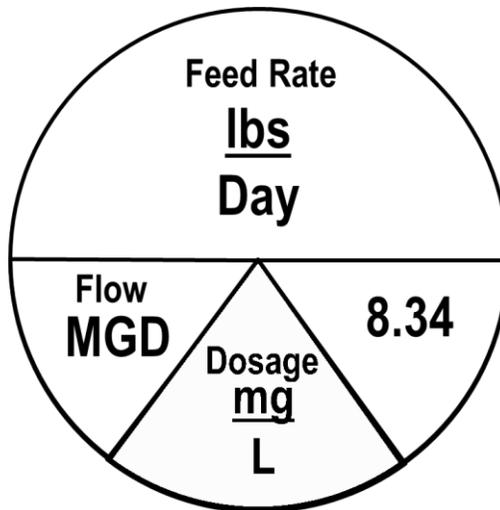
$$^{\circ}\text{C} = \frac{80^{\circ}\text{F}-32}{1.8} = \frac{48}{1.8} = \mathbf{27^{\circ}\text{C (rounded)}}$$

Equation #1: Solving for lbs/day using the Feed Rate Formula

$$\frac{? \text{ lbs}}{\text{day}} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times (8.34)$$

This feed rate formula is represented in the following diagram called the Davidson Pie which was created by Gerald Davidson, Manager, Clear Lake Oaks Water District, Clear Lake Oaks, CA.

Davidson Pie



Key Acronyms: MG = million gallons or MGD = million gallons per day

Practice Problem: If a water treatment plant is putting out 14 MGD, and dosing soda ash at the rate of 5 mg/l, how many pounds will they use every day?

$$\frac{? \text{ lbs}}{\text{day}} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times (8.34)$$

$$\frac{? \text{ lbs}}{\text{day}} = 14 \times 5 \times 8.34 = \underline{584}$$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

Practice Problem: If a water treatment plant is making 0.150 MGD, and the chlorine dose is 1.2 mg/l, how many pounds of gas chlorine will they use?

$$? \frac{\text{lbs}}{\text{day}} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times (8.34)$$

$$? \frac{\text{lbs}}{\text{day}} = (0.15)(1.2)(8.34) = \underline{1.5}$$

Converting from GPD to MGD before solving with the formula

Practice Problem: If a water treatment plant is making water at the rate of 300,000 gallons per day, and the chlorine dose is 2.0 mg/l, how many pounds of gas chlorine will they use daily?

Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times \frac{300,000 \text{ gallons}}{\text{day}} = 0.30 \text{ MGD}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.30 \times 2.0 \times 8.34 = \underline{5} \text{ lb/day}$$

Converting from GPM to MGD before solving with the formula

Practice Problem: A water treatment plant operates at the rate of 200 gallons per minute. They dose soda ash at 5 mg/L. How many pounds of soda ash will they use in a day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times \frac{200 \text{ gal}}{\text{minute}} \times 1440 \frac{\text{minutes}}{\text{day}} = \underline{0.288} \frac{\text{MG}}{\text{day}}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

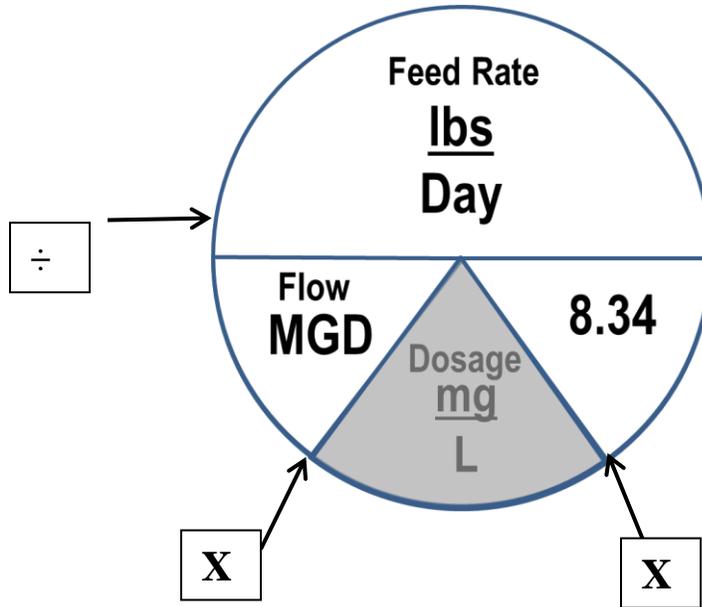
$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.288 \times 5 \times 8.34 = \underline{12} \text{ lb/day}$$

Equation #2: Solving for Dose (mg/L) using the Feed Rate Formula

An operator can also use the pie chart formula to calculate the dose if the known factors are the feed rate in pounds per day, and the flow rate.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, (lbs/ day)}}{\text{Flow(MGD)}(8.34)}$$



Practice Problem: A water treatment plant produces 150,000 gallons of water every day. It uses an average of 2 pounds of permanganate for iron and manganese removal. What is the dose of the permanganate?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(2) \text{ lbs/day}}{(0.15)(8.34)}$$

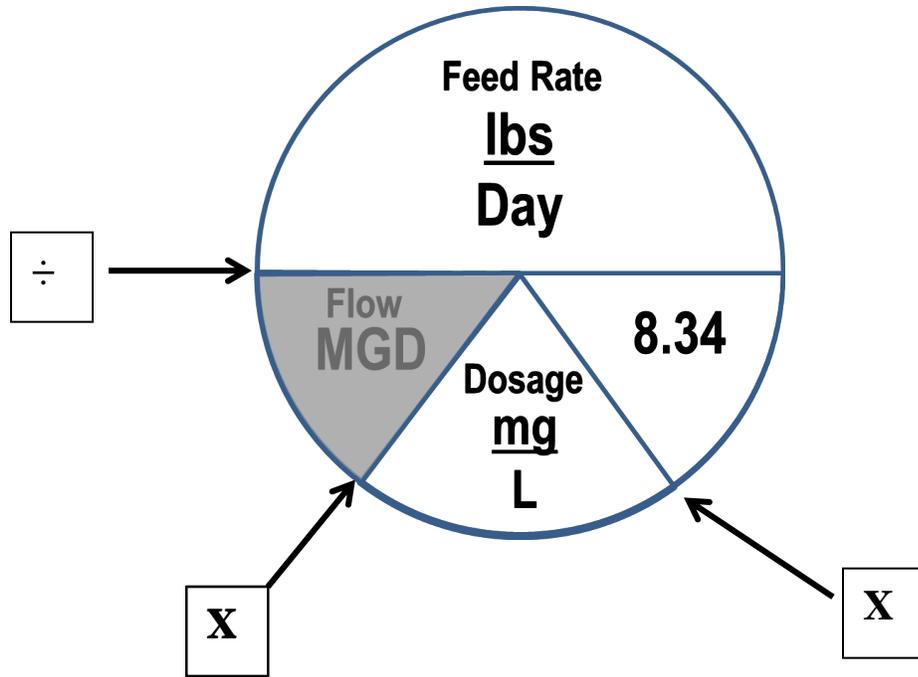
Step 3: Multiply 0.15 x 8.34 in the denominator = 1.25 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{2 \text{ (numerator)}}{1.25 \text{ (denominator)}} = \frac{1.56 \text{ mg}}{\text{L}}$$

Equation #3: Solving for Flow (MGD) using the Feed Rate Formula

Lastly, the pie chart formula can be used to calculate the flow if the dose and feed rate in pounds per day are known factors.

Example Problem: A water treatment plant uses 14 pounds of chlorine gas to treat their water daily. The chlorine dose is 1.5 mg/l. What is their flow rate in MGD?



Vertical Format: $\text{Flow, MGD} = \frac{\text{Feed Rate, lbs/per day}}{(\text{Dose, mg/L})(8.34)}$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

Practice Problem: A water treatment plant uses 8 pounds of chlorine daily and the dose is 17 mg/l. How many gallons are they producing?

Step 1: Set up the variables in vertical format and insert known values

$$? \text{ Flow (MGD)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Dose})(8.34)} = \frac{(8) \text{ lb/day}}{(17)(8.34)}$$

Step 2: Multiply 17 x 8.34 in the denominator = 141.78 (basic math rule)

$$\text{Step 3: Perform the FLOW division: } \frac{8 \text{ (numerator)}}{141.78 \text{ (denominator)}} = 0.056425 \text{ MGD}$$

Unit Cancellation Steps to solve for gallons/day

$$? \text{ gallons/day} = \frac{1,000,000 \text{ gallons}}{1 \text{ MG}} \times 0.056425 \frac{\text{MG}}{\text{day}} = 56,425 \frac{\text{gallons}}{\text{day}}$$

Quiz # 2

1. How many **pounds per day** will be required if the dose is 13 mg/L, and the flow treated is 1 MGD?

$$? \frac{\text{lbs}}{\text{day}} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times (8.34) = (1)(13)(8.34) = \underline{108 \text{ lbs/day}}$$

2. How many **pounds per day** will be required if the dose is 13 mg/l, and the flow is at the rate of 695 gpm?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times 695 \frac{\text{gal}}{\text{minute}} \times 1440 \frac{\text{minutes}}{\text{day}} = 0.068 \frac{\text{MG}}{\text{day}}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.068 \times 13 \times 8.34 = \underline{108 \text{ lb/day}}$$

**ANSWER KEY: 2017 Revised Basic Math
February 2017**

3. How many **pounds per day** will be needed to dose 335,000 gallons of water at 4 mg/L?

Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times \frac{335,000 \text{ gallons}}{\text{day}} = 0.335 \text{ MGD}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.335 \times 4.0 \times 8.34 = \underline{11} \text{ lb/day}$$

4. What is the **dose** if 2.5 MGD were treated with 31 pounds of chlorine?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(31) \text{ lbs/day}}{(2.5)(8.34)}$$

Step 3: Multiply 2.5 x 8.34 in the denominator = 20.85 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{31 \text{ (numerator)}}{20.85 \text{ (denominator)}} = \underline{1.5} \frac{\text{mg}}{\text{L}} \text{ (rounded)}$$

5. How many **pounds** will be required if the flow is 95 gpm, and the dose is 7mg/L, and the plant runs for 12 hours per day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times \frac{95 \text{ gal}}{\text{minute}} \times \frac{60 \text{ minutes}}{\text{hr}} \times \frac{12 \text{ hrs}}{\text{day}} = 0.0684 \frac{\text{MG}}{\text{day}} \text{ for 12 hrs}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.0684 \times 7 \times 8.34 = \underline{4} \text{ lb/day (rounded)}$$

Practice problems:

1. How many **pounds per day** will be used when the dose is 5 mg/L, and the flow rate is 350 gpm?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times 350 \frac{\text{gal}}{\text{minute}} \times 1440 \frac{\text{minutes}}{\text{day}} = 0.5 \frac{\text{MG}}{\text{day}}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.5 \times 5 \times 8.34 = \underline{21} \text{ lb/day (rounded)}$$

2. How many **pounds per day** will be needed if the flow rate is 80,000 gpd, and the dose is 25 mg/L?

Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = 1 \frac{\text{MG}}{1,000,000 \text{ gallons}} \times 80,000 \frac{\text{gallons}}{\text{day}} = 0.08 \text{ MGD}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.08 \times 25 \times 8.34 = \underline{17} \text{ lb/day}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

3. How many **pounds per day** will be used if the flow rate is 47 gpm through each filter, and there are 2 filters, and the dose is 7 mg/L?

Step 1: Determine **total flow rate** for both filters by multiplying by 2

$$47 \times 2 = 94 \text{ gpm}$$

Step 2: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = \frac{1 \text{ MG}}{1,000,000 \text{ gallons}} \times 94 \frac{\text{gal}}{\text{minute}} \times 1440 \frac{\text{minutes}}{\text{day}} = 0.135 \frac{\text{MG}}{\text{day}}$$

Step 3: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.135 \times 7 \times 8.34 = \underline{8} \text{ lb/day (rounded)}$$

4. How many **pounds per day** will be used if the flow rate is 50 gpm, the dose is 4 mg/L, and the plant operates for 16 hours each day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$? \frac{\text{MG}}{\text{day}} = \frac{1 \text{ MG}}{1,000,000 \text{ gallons}} \times 50 \frac{\text{gal}}{\text{minute}} \times 60 \frac{\text{minutes}}{\text{hr}} \times 16 \frac{\text{hrs}}{\text{day}} = 0.048 \frac{\text{MG}}{\text{day}} \text{ for 16 hrs}$$

Step 2: Use MGD in feed rate formula to solve for lbs/day

$$\text{Feed Rate, lbs per day} = \text{Flow(MGD)} \times \text{Dose(mg/L)} \times 8.34$$

$$0.048 \times 4 \times 8.34 = \underline{1.6} \text{ lb/day}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

5. What is the **dose** if the total water treated is 650,000 gallons, and 22 pounds of chemical was used?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(22) \text{ lbs/day}}{(0.65)(8.34)}$$

Step 3: Multiply 0.65 x 8.34 in the denominator = 20.85 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{22 \text{ (numerator)}}{5.42 \text{ (denominator)}} = \frac{4 \text{ mg (rounded)}}{\text{L}}$$

6. What is the **dose** if the plant uses 120 pounds of chemical each day to treat 1,350,000 gallons daily?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(120) \text{ lbs/day}}{(1.35)(8.34)}$$

Step 3: Multiply 1.35 x 8.34 in the denominator = 11.25 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{120 \text{ (numerator)}}{11.25 \text{ (denominator)}} = \frac{11 \text{ mg (rounded)}}{\text{L}}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

7. What is the **dose** if the operator uses 18 pounds of chemical to treat 650,000 gpd?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(18) \text{ lbs/day}}{(0.65)(8.34)}$$

Step 3: Multiply 0.65 x 8.34 in the denominator = 5.42 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{18 \text{ (numerator)}}{5.42 \text{ (denominator)}} = \frac{3.3 \text{ mg}}{\text{L}} \text{ (rounded)}$$

<p>Feed Rate Calculations Using <u>Flow</u> with a % Strength (i.e., % pure)</p> <p>Solution</p>
--

Practice Problem: A water plant uses 15% sodium hypochlorite to disinfect the water. The dose is 1.2 mg/L. They treat 0.25 million gallons per day. How many pounds of sodium hypochlorite will need to be fed?

Step 1: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ Pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.25)(1.2)(8.34) = 2.5 \text{ pounds of chlorine is required.}$$

Step 2: Calculate # of pounds of 15% solution needed to achieve Step 1 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{15\%}{100\%} = 0.15$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{2.5 \text{ pounds}}{0.15 \text{ (% purity as a decimal)}} = 16.7 \text{ pounds of 15\% hypochlorite.}$$

TIP: Answer will always be more pounds than Step 1 result because solution is not 100% pure.

ANSWER KEY: 2017 Revised Basic Math
February 2017

Practice Problem: A water plant doses liquid alum at 5 mg/L and treats 1.5 MGD. How many pounds of liquid alum will be required daily to do this? Liquid alum is 48½% pure.

Step 1: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ Pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (1.5)(5)(8.34) = \underline{62.55} \text{ pound alum.}$$

Step 2: Calculate # of pounds of 15% solution needed to achieve Step 1 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{48.5\%}{100\%} = \underline{0.485}$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{62.55 \text{ pounds}}{0.485 \text{ (\% purity as a decimal)}} = \underline{128.96} \text{ or } 129 \text{ pounds of liquid alum.}$$

Feed Rate Calculations Using Volume with a % Strength (i.e., % pure) Solution

Practice Problem: Calculate the amount of calcium hypochlorite to dose a 500,000 gallon storage tank to a dose of 25 mg/L using granular calcium hypochlorite that indicates it is 65% chlorine.

Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.

$$? \text{ MG} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times (500,000) \text{ gal} = \underline{0.5} \text{ MG}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ lbs} = \text{volume(MG)} \times \text{dose(mg/L)} \times 8.34 = (0.5)(25)(8.34) = \underline{104.25} \text{ pounds of chlorine is required.}$$

Step 3: Calculate # of pounds of 65% solution needed to achieve Step 2 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{65\%}{100\%} = \underline{0.65}$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{104.25 \text{ pounds}}{0.65} = \underline{160.39} \text{ pounds of 65\% calcium hypochlorite.}$$

Calculating “Active Ingredient” Weight



Active ingredient weight is the number of pounds of “active ingredient” per gallon of a % solution that cause a chemical reaction.

- This “active ingredient” weight value is then used in a calculation with the 100% pure “lbs/day” feed rate to determine the “gal/day” feed rate.

Calculating the Weight of the “Active ingredient” of a % Solution Chemical

Practice Problem: How many pounds of caustic soda are there in a gallon of caustic soda that is 25% pure that has a specific gravity of 1.28?

Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical

Weight, lbs/gal = (Specific gravity of substance) x (weight of a gallon of water)

$$1.28 \quad \times \quad 8.34 \frac{\text{pounds}}{\text{gallon}} = \frac{10.67 \text{ pounds}}{\text{gallon}}$$

Step 2: Determine the “active ingredient” weight of the caustic soda based on the % purity of solution

a) Convert % purity of solution into a decimal:

$$\frac{25\%}{100\%} = \frac{0.25}{1}$$

b) Multiply the weight of a gallon (from step 1) by the % purity of the product (as a decimal).

$$10.67 \frac{\text{pounds}}{\text{gallon}} \times 0.25 = \underline{2.66} \text{ pounds of caustic soda in a gallon of 25\% caustic soda solution}$$

This “active ingredient” weight provides the pounds of available caustic soda that is found in each gallon of 25% caustic soda solution. Within the 10.67 pounds of 25% caustic solution, there are 2.66 pounds of active ingredients.

Using “Active Ingredient” Weight to Convert Feed Rate from lbs/day to gal/day

Practice Problem: A water plant uses sodium hypochlorite (12.5%) to disinfect the water which provides 1.2 lbs/gal of available chlorine (“active ingredient” weight). The chlorine dosage is 1.6 mg/L. They treat 600,000 gallons per day. How many **gallons** of sodium hypochlorite will need to be fed?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.

$$? \text{ MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{600,000 \text{ gal}}{1 \text{ day}} = \underline{0.6} \text{ MGD}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.6)(1.6)(8.34) = \underline{8} \text{ pounds of chlorine is required.}$$

Step 3: Use “active ingredient” weight with unit cancellation steps to convert lbs/day to **gal/day**

Active Ingredient Weight
of 12.5% hypo solution

Feed Rate of 100% pure chlorine

$$? \frac{\text{gal}}{\text{day}} = \frac{1 \text{ gallon}}{1.2 \text{ lbs}} \times \frac{8 \text{ lbs}}{\text{day}} = \underline{6.67} \frac{\text{gal}}{\text{day}}$$

NOTE: When you are given the “active ingredient” weight of a solution to solve a feed rate problem, you do not need to use the % purity factor because it was used to derive the active ingredient weight.

ANSWER KEY: 2017 Revised Basic Math
February 2017

Quiz: 3

1. How many **pounds** of alum (48.5 %) are required to treat 0.75 MGD with a dose of 12 mg/L?

Step 1: Solve for pounds (feed rate) for 100 % pure chemical (no impurities).

? pounds per day = flow x dose x 8.34 = (0.75)(12)(8.34) = **75** pounds of chlorine is required.

Step 2: Calculate # of pounds of 65% solution needed to achieve Step 2 feed rate.

- a) Convert % purity of solution into a decimal:

$$\frac{48.5\%}{100\%} = 0.485$$

- b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{75 \text{ pounds}}{0.485} = 155 \text{ pounds of 48.5\% alum.}$$

0.485 (% purity as a decimal)

ANSWER KEY: 2017 Revised Basic Math
February 2017

2. How many **pounds** of calcium hypochlorite (65 %) are needed to treat 500,000 gallons per day with a dose of 2 mg/L?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.

$$? \text{ MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{500,000 \text{ (gal)}}{1 \text{ day}} = \mathbf{0.5 \text{ MGD}}$$

Step 2: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.5)(2)(8.34) = \mathbf{8.34} \text{ pounds of chlorine is required.}$$

Step 3: Calculate # of pounds of % solution needed (in this example, 65%) to achieve Step 2 feed rate.

- a) Convert % purity of solution into a decimal:

$$\frac{65\%}{100\%} = \mathbf{0.65}$$

- b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{8.34 \text{ pounds}}{0.65} = \mathbf{12.8} \text{ pounds of 65\% calcium hypochlorite.}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

3. How many **pounds** of sodium hypochlorite (12½ %) are needed to treat a flow of 150 gallons per minute at a dose of 0.7 mg/L?

Step 1: Convert flow in gallons (per minute) into MGD so that the feed rate (lbs/day) formula can be used.

$$? \text{MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{\text{volume of flow (gal)}}{1 \text{ min}} \times \frac{1440 \text{ min}}{\text{day}}$$

$$? \frac{\text{MG}}{\text{day}} = \frac{1 \text{ MG}}{1,000,000 \text{ gallons}} \times \frac{150 \text{ gal}}{\text{minute}} \times \frac{1440 \text{ minutes}}{\text{day}} = 0.216 \frac{\text{MG}}{\text{day}}$$

Step 2: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.216)(0.7)(8.34) = \mathbf{1.26} \text{ pounds of chlorine is required.}$$

Step 3: Calculate # of pounds of % solution needed (in this example, 65%) to achieve Step 2 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{12.5\%}{100\%} = 0.125$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{1.26 \text{ pounds}}{0.125} = \mathbf{10} \text{ pounds of 12.5\% sodium hypochlorite.}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

4. How many **pounds** of caustic soda are needed to dose water at 17 mg/L if you are treating 1,400,000 gallons per day? The caustic soda concentration is 50 percent.

Step 1: Solve for pounds (feed rate) for 100 % pure chemical (no impurities).

? pounds per day = flow x dose x 8.34 = (1.4)(17)(8.34) = **198** pounds of chlorine is required.

Step 2: Calculate # of pounds of 65% solution needed to achieve Step 2 feed rate.

- a) Convert % purity of solution into a decimal:

$$\frac{50\%}{100\%} = 0.5$$

- b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{198 \text{ pounds}}{0.5 \text{ (\% purity as a decimal)}} = 397 \text{ pounds of 50\% PAC}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

5. How many **pounds** of chlorine gas are required to treat 750,000 gallons of water to a dose of 50 mg/L for a 24 hour period?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.

$$? \text{ MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{750,000 \text{ gal}}{1 \text{ day}} = \mathbf{0.75 \text{ MGD}}$$

Step 2: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.75)(50)(8.34) = \mathbf{313 \text{ pounds of chlorine is required.}}$$

6. A treatment plant uses 12.5% hypochlorite to disinfect the water. The required hypochlorite dosage is 2 mg/L and the plant flow is 300,000 gpd. How many **gallons** of 12.5% hypochlorite are required (12.5% hypo has 1.25 lbs/gal available chlorine)?

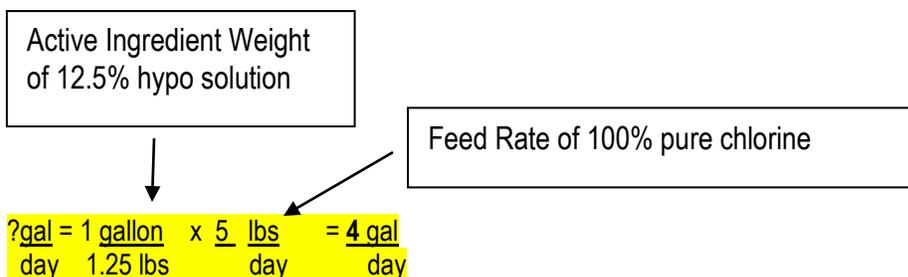
Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.

$$? \text{ MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{300,000 \text{ gal}}{1 \text{ day}} = \mathbf{0.3 \text{ MGD}}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (0.3)(2)(8.34) = \mathbf{5 \text{ pounds of chlorine is required.}}$$

Step 3: Use "active ingredient" weight with unit cancellation steps to convert lbs/day to **gal/day**



Calculating the Weight of a Solution

Another consideration in water chemistry calculations is the weight of the product being used. For example, the weight of a gallon of water is 8.34 pounds. We learned earlier that there are 7.48 gallons in a cubic foot of water.

Practice Problem: What would be the weight of 100 gallons of water?

$$? \text{ lbs} = 8.34 \frac{\text{lbs}}{\text{gal}} \times 100 \text{ gal} = \underline{834} \text{ lbs}$$

Using Specific Gravity to calculate the weight of a solution

To calculate the weight of various chemicals we need to factor in the specific gravity of the chemical being used. Specific gravity is the weight of a substance compared to the weight of a gallon of water. Specific gravity information is found on the Safety Data Sheets (SDS) and is used to calculate the weight of a substance.

$$\text{Total Weight, lbs/gal} = (\text{Specific gravity of substance}) \times (\text{weight of a gallon of water})$$

Practice Problem: What is the weight of a gallon of sodium hypochlorite if the specific gravity is 1.11?

$$\text{Weight, lbs/gal} = (\text{Specific gravity of substance}) \times (\text{weight of a gallon of water})$$

$$? \frac{\text{lbs}}{\text{gal}} = 1.11 \times 8.34 \frac{\text{lbs}}{\text{gal}} = \underline{9.26} \frac{\text{lbs}}{\text{gal}}$$

Practice Problem: What is the weight of a gallon of crankcase oil if the specific gravity is 0.89?

$$\text{Weight, lbs/gal} = (\text{Specific gravity of substance}) \times (\text{weight of a gallon of water})$$

$$? \frac{\text{lbs}}{\text{gal}} = 0.89 \times 8.34 \frac{\text{lbs}}{\text{gal}} = \underline{7.4} \frac{\text{lbs}}{\text{gal}}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

Calculating the weight of a drum

If you want to determine the weight of a drum or tank of solution, you must include that volume in your calculation.

$$\text{Drum Weight, lbs} = (\text{gallons of drum or tank}) \times (\text{S.G.}) \times (8.34 \text{ lbs/gal})$$

Practice Problem: What would be the weight of a 50 gallon drum of 50% caustic soda if the specific gravity of the product is 1.53

$$\text{Drum Weight, lbs} = (\text{gallons of drum or tank}) \times (\text{S.G.}) \times (8.34 \text{ lbs/gal})$$

? Drum weight, lbs = $50 \times 1.53 \times 8.34 = \underline{638}$ lbs.

Calculating “Active Ingredient” Weight

Practice Problem: What is the active ingredient weight of 48.5% alum that has a specific gravity of 1.33.

Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical

Weight, lbs/gal = (Specific gravity of substance) x (weight of a gallon of water)

$$1.33 \times 8.34 \frac{\text{lbs}}{\text{gal}} = 11.09 \frac{\text{lbs}}{\text{gal}}$$

Step 2: Determine the “active ingredient” weight of the solution based on the % purity of solution

a) **Convert % purity of solution into a decimal:**

$$\frac{48.5}{100} = 0.485$$

b) **Multiply the weight of a gallon (from step 1) by the % purity of the product (as a decimal).**

$$11.09 \frac{\text{lbs}}{\text{gal}} \times 0.485 = \underline{5.37} \text{ pounds of available alum in a gallon of 48.5 \% alum}$$

Calculating the active ingredient weight of a drum of solution

You can also calculate how many pounds of active ingredients there are in drum or tank of a liquid product.

$$? \text{ lbs of active ingredient within drum} = \text{drum volume (gal)} \times \text{active ingredient weight (lbs/gal)}$$

Example Problem: How many pounds of active ingredient are there in a 55 gallon drum of liquid alum if the product is 48½ percent pure with a specific gravity of 1.33 and the active ingredient weight is 5.37 lbs of alum/gal of product?

$$? \text{ lbs of active ingredient within drum} = \text{active ingredient weight (lbs/gal)} \times \text{drum volume (gal)}$$

$$? \text{ lbs of active ingredient within drum} = 5.37 \frac{\text{lbs}}{\text{gal}} \times 55 \text{ gal}$$

$$= \underline{295.8} \text{ lbs of active ingredient (alum) within the 48.5\% solution}$$

Alternative Method of Calculating Active Ingredient Weight of a Drum:

Example Problem: How many pounds of active ingredient are there in a 55 gallon drum of liquid alum if the product is 48½ percent pure with a specific gravity of 1.33 and the active ingredient weight is 5.37 lbs of alum/gal of product?

Step 1: Solve weight equation (lbs/gal) for the drum

$$\text{Drum Weight, lbs} = (\text{gallons of drum or tank}) \times (\text{S.G.}) \times (8.34 \text{ lbs/gal})$$

$$? \text{ Drum Weight, lbs} = 55 \text{ gal} \times 1.33 \times 8.34$$

$$= 610 \text{ lbs}$$

Step 2: Determine the “active ingredient” weight of the solution based on the % purity of solution

a) Convert % purity of solution into a decimal:

$$\frac{48.5}{100} = 0.485$$

b) Multiply the weight of the drum (from step 1) by the % purity of the product (as a decimal).

$$610 \text{ lbs} \times 0.485 = \underline{295.8} \text{ lbs of active ingredient (alum) within the 48.5\% alum solution}$$



Math Concept Exercise

1. In order to use the Feed Rate formula which is $\text{lbs/day} = \text{Flow} \times \text{Dosage} \times 8.34$, name the units of measurement for the **flow**:

a) MGD

b) gpm

c) gpd

d) All of the above units can be used

ANSWER KEY: 2017 Revised Basic Math
February 2017

2. If you have a flow in **gpm**, what calculation do you use to convert it to **MGD**?
- a) Multiply gpm X 24 and divide by 1,000,000
 - b) Multiply gpm x 60 and divide by 1,000,000
 - c) Multiply gpm x 1440 and divide by 1,000,000**
 - d) Divide flow in gpm by 1,000,000
3. If you have a flow in **gpd**, what calculation do you use to convert it to **MGD**?
- a) Divide flow in gpd by 100
 - b) Divide flow in gpd by 10,000
 - c) Divide flow in gpd by 100,000
 - d) Divide flow in gpd by 1,000,000**
4. When using “active ingredient” weight to solve for “gallons”, what calculation do you use?
- a) ? gals = 1 gal X “lbs” (as a % solution feed rate)**
1.63 lbs
 - b) ? gals = 1.63 lbs X “lbs” (as a % solution feed rate)
gal

Final Quiz :

1. What is the **volume in gallons** of a water tank that is 25 feet in diameter, and filled to a depth of 17 feet?

Step 1: Solve the volume equation in ft³:

$$V = 0.785(\text{Dia})^2(H)$$

$$V = 0.785(25 \text{ ft})(25 \text{ ft})(17 \text{ ft}) = \underline{8340.6} \text{ ft}^3$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = 7.48 \frac{\text{gal}}{1 \text{ ft}^3} \quad \times \underline{8340.6} \text{ ft}^3 = \underline{62,388} \text{ gallons (rounded)}$$

2. What is the **volume in gallons** in a sedimentation basin that is 50 feet long, 35 feet wide, and filled to a depth of 12 feet?

Step 1: Solve the volume equation in ft³:

$$V = (L)(W)(H)$$

$$V = (50 \text{ ft})(35 \text{ ft})(12 \text{ ft}) = \underline{21,000} \text{ ft}^3$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = 7.48 \frac{\text{gal}}{1 \text{ ft}^3} \quad \times \underline{21,000} \text{ ft}^3 = \underline{157,080} \text{ gallons (rounded)}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

3. How many **pounds** of chemical will be fed if the dose required is 13 mg/L, and the amount of water to be treated is 175,000 gallons per day?

Step 1: Convert flow (in gallons) into MG so that the feed rate (lbs) formula can be used.

$$? \text{MG} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times (175,000) \text{ gal} = \underline{0.175 \text{ MG}}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ lbs} = \text{volume(MG)} \times \text{dose(mg/L)} \times 8.34 = (0.175)(13)(8.34) = \underline{19} \text{ pounds of chlorine is required. (rounded)}$$

4. What is the **dose** if a water plant used 40 pounds of chemical, and treated 1.2 million gallons of water?

Step 1: Set up the variables in vertical format.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)}$$

Step 2: Insert known values into equation.

$$? \text{ Dose (mg/L)} = \frac{\text{Feed Rate, lbs/day}}{(\text{Flow, MGD})(8.34)} = \frac{(40) \text{ lbs/day}}{(1.2)(8.34)}$$

Step 3: Multiply 1.2 x 8.34 in the denominator = 10 (basic math rule)

$$\text{Step 4: Perform the DOSE division: } \frac{40 \text{ (numerator)}}{10 \text{ (denominator)}} = \underline{4 \frac{\text{mg}}{\text{L}}}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

5. The target dose for a system is 1.2 mg/L. They are treating an average of 300,000 gallons each day. How many **lbs** of sodium hypochlorite (12½ %) will they need to feed?

Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.

$$?MG = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times (300,000) \text{ gal} = \underline{0.3 \text{ MG}}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ lbs} = \text{volume(MG)} \times \text{dose(mg/L)} \times 8.34 = (0.3)(1.2)(8.34) = \underline{3 \text{ pounds of chlorine is required.}}$$

Step 3: Calculate # of pounds of 65% solution needed to achieve Step 2 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{12.5\%}{100\%} = \underline{0.125}$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{3 \text{ pounds}}{0.125} = \underline{24 \text{ pounds of 65\% calcium hypochlorite.}}$$

6. The specific gravity of the hypochlorite is 1.11. If the system needs to feed 24 pounds of hypochlorite, how many **gallons** will that require?

Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical

Weight, lbs/gal = (Specific gravity of substance) x (weight of a gallon of water)

$$1.11 \times 8.34 \frac{\text{pounds}}{\text{gallon}} = 9.26 \frac{\text{pounds}}{\text{gallon}}$$

Step 2: Use weight of gallon of hypochlorite solution with unit cancellation steps to convert lbs/day to gal/day

$$? \frac{\text{gal}}{\text{day}} = \frac{1 \text{ gallon}}{9.26 \text{ lbs}} \times \frac{24 \text{ lbs}}{\text{day}} = \underline{2.6 \text{ gal (rounded)}}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

7. How many **pounds** of chlorine will be needed to disinfect a 250,000 gallon tank if a 50 mg/L dose is required?

Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.

$$? \text{MG} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times (250,000) \text{ gal} = \underline{0.25 \text{ MG}}$$

Step 2: Solve for pounds per day (feed rate) for 100 % pure chemical (no impurities).

$$? \text{ lbs} = \text{volume(MG)} \times \text{dose(mg/L)} \times 8.34 = (0.25)(50)(8.34) = \underline{104.25} \text{ pounds of chlorine is required.}$$

8. What is the **weight** of the water that is in a container one foot long, one foot wide, and filled to a depth of 1 foot?

Step 1: Solve the volume equation in ft³:

$$V = (L)(W)(H)$$

$$V = (1 \text{ ft})(1 \text{ ft})(1 \text{ ft}) = \underline{1} \text{ ft}^3$$

Step 2: Convert ft³ into gallons:

$$? \text{ gal} = \frac{7.48 \text{ gal}}{1 \text{ ft}^3} \times \underline{1} \text{ ft}^3 = \underline{7.48} \text{ gallons}$$

Step 3: Convert gallons into lbs.

$$? \text{ lbs} = 8.34 \frac{\text{lbs}}{\text{gal}} \times 7.48 \text{ gal} = \underline{62.4} \text{ lbs}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

- 9 How many **pounds** of aluminum sulfate (48.5%) are required to dose water at 21 mg/L if the amount of water treated is 2 MGD?

Step 1: Solve for pounds per day (feed rate) for 100% pure chemical (no impurities).

$$? \text{ Pounds per day} = \text{flow} \times \text{dose} \times 8.34 = (2)(21)(8.34) = 350.28 \text{ pound alum.}$$

Step 2: Calculate # of pounds of 48.5% solution needed to achieve Step 1 feed rate.

a) Convert % purity of solution into a decimal:

$$\frac{48.5\%}{100\%} = 0.485$$

b) Then divide the pounds needed (feed rate of 100% pure chemical) by the % purity of the solution (as a decimal).

$$\frac{350.28 \text{ pounds}}{0.485 \text{ (\% purity as a decimal)}} = \underline{722} \text{ pounds of liquid alum.}$$

10. Convert a flow of 65 gallons per minute to the **MGD** unit.

$$? \text{ MGD} = \frac{1 \text{ MG}}{1,000,000 \text{ gal}} \times \frac{\text{volume of flow (gal)}}{1 \text{ min}} \times \frac{1440 \text{ min}}{\text{day}}$$

$$? \frac{\text{MG}}{\text{day}} = \frac{1 \text{ MG}}{1,000,000 \text{ gallons}} \times \frac{65 \text{ gal}}{\text{minute}} \times \frac{1440 \text{ minutes}}{\text{day}} = 0.0936 \frac{\text{MG}}{\text{day}}$$

ANSWER KEY: 2017 Revised Basic Math
February 2017

11. How **high (in ft)** is the water column if the pressure at the bottom measures 40 psi?

$$? \text{ ft} = \frac{2.31 \text{ ft}}{1 \text{ psi}} \times 40 \text{ psi} = \underline{92 \text{ ft}}$$

12. Convert 17° C to °F.

$$^{\circ}\text{F} = (^{\circ}\text{C} \times 1.8) + 32$$

$$^{\circ}\text{F} = (17 \times 1.8) + 32 = 31 + 32 = \underline{63^{\circ}\text{F}}$$

13. What is the % **unaccounted water** if a system records the following readings:

The master meter reading is 1,500,000 gallons.

The meter reading total is 965,000 gallons

Another 100,000 gallons were used for flushing, and 35,000 gallons were metered at a blow-off.

Step 1: Add total gallons accounted for (billed, blow-off, and flushing)

$$\text{Gallons Accounted for} = \underline{965,000} \text{ (billed)} + \underline{35,000} \text{ (blow-off)} + \underline{100,000} \text{ (flushing)} = \underline{1,100,000}$$

Step 2: Subtract “accounted for” from total produced to find “Unaccounted for”

$$1,500,000 - \underline{1,100,000} \text{ (Step 1 Accounted for)} = \underline{400,000} \text{ (Unaccounted for)}$$

Step 3: Divide “Unaccounted for” by total produced and multiply by 100 to equal the % unaccounted for

$$\frac{\underline{400,000} \text{ (Step 2 Unaccounted For)}}{1,500,000 \text{ (Total Produced)}} = \underline{0.266} \times 100 = \underline{27\%} \text{ Unaccounted for (rounded)}$$