## ANSWER KEY: 2020 Revised Basic Math

October 2020

## 2020 Revised Basic Math Answer Key

## Explanation of diagonal movement and an example:

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$5 \mathrm{X}=20$

Question \#1 regarding Example \#1: Is the $\boldsymbol{X}$ in the numerator? YES
Question \#2 regarding Example \#1: Is the $X$ alone on one side of the equation? NO
How do we use diagonal movement to place $\boldsymbol{X}$ alone on one side of the equation?

Answer:

- Divide both sides by " 5 " to get $X$ alone and treat both sides of the equation equally. Notice that the 5 was moved from the top of the left side to the bottom of the right side of the equation - a diagonal move.
$\frac{5 X}{5}=\frac{20}{5}$

FINAL ANSWER: $20 \div 5=\underline{4}$

## Practice Problem: Steps to solving problems using unit cancellation

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Practice Problem: How many minutes are there in a day?
Problem Set Up
List all known and unknown data.
Unknown: ? $\frac{\min }{\text { day }} \quad$ Known: $60 \frac{\mathrm{mins}}{\mathrm{hr}} \quad 24 \frac{\mathrm{hrs}}{1}$

Step 1: List unknown data including units in vertical format followed by an equal sign.
$? \frac{\min }{d a y}=$

Step 2: Find data (known or a conversion) that has the same numerator unit as the unknown numerator.
?lace it to the right of th
$\frac{\min }{\text { day }}=60 \frac{(\mathrm{~min}}{\mathrm{hr}}$

Steps 3 and 4: To cancel unwanted denominator unit, find data (known or a conversion) that has the same numerator unit. Place it to the right of data used in Step 2. Place a multiplication sign between each piece of data. Continue to place data (known or a conversion) into equation to systematically cancel all unwanted units until only the unknown denominator units remain.


Step 5: Multiply the values of all numerators and place this value in the numerator of the answer. Multiply the values of all denominators and place this value in the denominator of the answer. Divide to calculate the final answer.

$$
? \frac{\mathrm{~min}}{\text { day }}=60 \frac{\mathrm{~min}}{1 \mathrm{hf}} \times 24 \frac{\mathrm{hrs}}{1 \mathrm{day}}=1440 \underset{\mathrm{~min}}{\text { day }} \longleftarrow \longleftarrow \begin{aligned}
& \text { These are the correct units in both } \\
& \text { numerator and denominator }
\end{aligned}
$$

## Pressure/Height Conversions

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Practice Problem calculating psi: The water level at the top of a fully filled water standpipe is 150 feet above the elevation of a water tap. The tank contains 50,000 gallons of water. What is the approximate pressure at the tap?

$$
? \mathrm{psi}=\frac{1 \mathrm{psi}}{2.31 \mathrm{ft}} \times \underline{150 \mathrm{\#}}=\underline{150 \mathrm{psi}} \frac{64.9}{2.31} \mathrm{psi}
$$

Note: Remember pressure is not affected by volume, only height.

Practice Problem calculating height in ft: An elevated tank records a pressure of 25 psi, what is the height of water in the tank?

To calculate height in ft from psi :
$? \mathrm{ft}=\underline{2.31 \mathrm{ft}} \times 25 \mathrm{psi}=\underline{58} \mathrm{ft}$
1 psi

## Temperature Conversions

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Practice Problem Solving for ${ }^{\circ} \mathrm{C}$ : Convert $60^{\circ} \mathrm{F}$ into ${ }^{\circ} \mathrm{C}$
${ }^{\circ} \mathrm{C}=\frac{{ }^{\circ} \mathrm{F}-32}{1.8} \quad 60-32=\underline{\mathbf{2 8}} \frac{1.8}{1.8}{ }^{\circ} \mathrm{C}$

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Practice Problem Solving for \({ }^{\circ} \mathrm{F}\) : Convert \(20^{\circ} \mathrm{F}\) into \({ }^{\circ} \mathrm{C}\)
\({ }^{\circ} \mathrm{F}=\left({ }^{\circ} \mathrm{C}\right.\) X 1.8) +32
\({ }^{\circ} \mathrm{F}=20 \times 1.8=36+32=\underline{68}{ }^{\circ} \mathrm{F}\)
```


## Unaccounted Water Calculation

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Practice Problem: In one month a water system produced $5,500,000$ gallons of water. Of the total water, 4,500,000 gallons were billed, 250,000 were used for fire protection and 200,000 gallons were used for flushing. What is the total unaccounted for water loss percentage for this month?

Step 1: Add total gallons accounted for (billed, fire protection and flushing)
Gallons Accounted for $=\underline{4,500,000}$ (billed) $+\underline{\mathbf{2 5 0 , 0 0 0}}$ (fire protection) $+\underline{\mathbf{2 0 0}, 000}$ (flushing) $=\underline{4,950,000}$
Step 2: Subtract "accounted for" from total produced to find "Unaccounted for"
$5,500,000-\underline{4,950,000}($ Step 1 Accounted for) $=\underline{\mathbf{5 5 0 , 0 0 0}}$ (Unaccounted for)
Step 3: Divide "Unaccounted for" by total produced and multiply by 100 to equal the \% unaccounted for
$\underline{550,000}$ (Step 2 Unaccounted For) $=\underline{\mathbf{0 . 1}} \times 100=\underline{10} \%$ Unaccounted for 5,500,000 (Total Produced)

## Area of a Rectangle

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Practice Problem: The sedimentation basin for the filtration plant is $25 \mathrm{ft} . \mathrm{x} 15 \mathrm{ft}$. What is the area in square feet?

Area $=(\mathrm{L}) X(\mathrm{~W})=25 \mathrm{ft} . \times 15 \mathrm{ft} .=\underline{375} \mathrm{ft}^{2}$

## Area of a Rectangle - Converting inches to feet

Practice Problem: The filter unit at the plant is 15 ft . 6 inches long, and 15 ft . 6 inches wide. What is the area of the filter?

Step 1: Convert inches to feet
The first step in solving this problem is to change the inch units to feet units. The tank is 15 feet. 6 inches long, by 15 feet 6 inches wide.

$$
? \mathrm{ft}=1 \mathrm{ft} \times 6 \mathrm{inches}=\underline{6}=\underline{0.5} \mathrm{ft}
$$

12 inches- 12
Step 2: Add 0.5 ft to the length and the width and insert into equation and multiply $\mathrm{L} X \mathrm{X}$.
Area $=(\mathrm{L}) X(\mathrm{~W})=15.5 \mathrm{ft} \times 15.5 \mathrm{ft}=\underline{\mathbf{2 4 0 . 2 5}} \mathrm{ft}^{2}$

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## Area of a Circle

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Practice Problem: The day tank for the coagulant is 4 feet in diameter, what is the area in square feet?
Area $=(0.785)(\text { Diameter })^{2}=(0.785)(4 \mathrm{ft})(4 \mathrm{ft})=\underline{12.56} \mathrm{ft}^{2}$

## Area of a Circle - Converting inches to feet

Practice Problem: The chemical feed tank is 20 inches in diameter, what is the area of the chemical feed tank?

Step 1: Convert inches to feet
$? \mathrm{ft}=1 \underline{\mathrm{tt}} \times 20 \underline{\text { inches }}=\underline{1.67} \mathrm{ft}$ 12 inches

Step 2: Insert diameter (in ft) into area formula and do the math.
Area $=(0.785)(\mathrm{D})^{2}=(0.785)(1.67 \mathrm{ft})(1.67 \mathrm{ft})=\underline{\mathbf{2} .19} \mathrm{ft}^{2}$

## Volume of a Rectangle in $\mathrm{ft}^{\mathbf{3}}$

The formula for volume of a rectangle is length X width X height or depth, or $(\mathrm{L})(\mathrm{W})(\mathrm{H}$ or D$)$
Note: For this equation, the terms "height" and "depth" are interchangeable.
Practice Problem: What is the volume of a clearwell that is 40 feet long, by 40 feet wide, by 12 feet deep?
$V=(L)(W)(D)=(40 \mathrm{ft})(40 \mathrm{ft})(12 \mathrm{ft})=\underline{19,200} \mathrm{ft}^{3}$

## Volume of a Circular Tank in $\mathrm{ft}^{\mathbf{3}}$

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Example Problem: What is the volume in cubic feet of a tank that is 22 feet in diameter, and filled to 8 feet deep?
$\mathrm{V}=0.785(\mathrm{Dia})^{2}(\mathrm{H})$
$V=0.785(22 \mathrm{ft})(22 \mathrm{ft})(8 \mathrm{ft})$
$V=3039.5 \mathrm{ft}^{3}$ or $3040 \mathrm{ft}^{3}$

## Volume of a Circular Tank in $\mathrm{ft}^{\mathbf{3}}$ - Converting inches to feet

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Practice Problem: What is the volume of a day tank that is filled to 3 feet, and is 20 inches wide?
Step 1: Convert inches to feet

$$
? \mathrm{ft}=\frac{1 \mathrm{ft}}{12} \text { inches } 20 \text { inches }=\underline{1.67} \mathrm{ft}
$$

Step 2: Insert diameter (in ft) into volume formula and do the math.
$V=0.785(1.67 \mathrm{ft})(1.67 \mathrm{ft})(3 \mathrm{ft})=\underline{6.6} \mathrm{ft}^{3}$

## Volume of a Rectangular Tank - Converting $\mathrm{ft}^{3}$ to gallons

The problems in the previous examples requested the volume measured in units of cubic feet. More often, the volumes are measured in gallons. The conversion factor to go from cubic feet to gallons is:
$1 \mathrm{ft}^{3}=7.48$ gallons
To convert $\mathrm{ft}^{3}$ to gallons, use this equation:
Gallons $=$ volume in $\mathrm{ft}^{3} \times 7.48$

## $1 \mathrm{ft}^{3}$ <br> 7.48 gallons

Therefore, if we were asked to calculate the volumes in the previous problems in gallons instead of cubic feet, the solution would require one extra step.

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Practice Problem: What is the volume, in gallons, of a tank 40 feet square and filled to 12 feet deep?
Step 1: Solve the volume equation in $\mathrm{ft}^{3}$ :
$V=(L)(W)(D)=(40 \mathrm{ft})(40 \mathrm{ft})(12 \mathrm{ft})=\underline{19,200} \mathrm{ft}^{3}$
Step 2: Convert ft ${ }^{3}$ into gallons:
$? \mathrm{gal}=7.48 \mathrm{gal} \quad X \underline{19,200} \mathrm{ft}^{3}=\underline{143,616}$ gallons

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## Volume of a Circular Tank - Converting $\mathrm{ft}^{3}$ to gallons

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Practice Problem: What is the volume, in gallons, of a day tank that is filled to 3 feet, and is 20 inches wide?

Step 1: Convert inches to feet

$$
? \mathrm{ft}=\frac{1 \mathrm{ft}}{12} \mathrm{inches} .20 \text { inches }=\underline{1.67} \mathrm{ft}
$$

Step 2: Insert diameter (in ft) into volume formula and do the math.
$V=0.785(1.67 \mathrm{ft})(1.67 \mathrm{ft})(3 \mathrm{ft})=\underline{\mathbf{6 . 6}} \mathrm{ft}^{3}$
Step 3: Convert ft ${ }^{3}$ into gallons:
$? \mathrm{gal}=7.48 \underline{\mathrm{gal}} \quad \times \underline{\mathrm{ft}^{3}} \quad \mathrm{ft}^{3}=\underline{49.3}$ gallons

## QUIZ \# 1

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1. What is the volume in $\mathrm{ft}^{3}$, of a sedimentation basin that is 22 feet long, and 15 feet wide, and filled to 10 feet?
$V=(\mathrm{L})(\mathrm{W})(\mathrm{H})=(22 \mathrm{ft})(15 \mathrm{ft})(10 \mathrm{ft})=\underline{3300 \mathrm{ft}^{3}}$
2. What is the volume in gallons of a clear well that is 35 feet long, 30 feet wide, and filled to 18 feet?

Step 1: Solve the volume equation in $\mathrm{ft}^{3}$
$V=(\mathrm{L})(\mathrm{W})(\mathrm{D})=(35 \mathrm{ft})(30 \mathrm{ft})(18 \mathrm{ft})=\underline{18900} \mathrm{ft}^{3}$
Step 2: Convert $\mathrm{ft}^{3}$ into gallons:

$$
? \mathrm{gal}=\frac{7.48 \mathrm{gal}}{1 \mathrm{f}^{3}} \quad X \underline{18900} \#^{3}=\underline{141,372} \text { gallons }
$$

3. What is the volume in gallons of a storage tank that is 20 feet in diameter, and filled to 18 feet?

Step 1: Solve the volume equation in $\mathrm{ft}^{3}$ :
$\mathrm{V}=0.785(\mathrm{Dia})^{2}(\mathrm{H})$
$V=0.785(20 \mathrm{ft})(20 \mathrm{ft})(18 \mathrm{ft})=\underline{5652} \mathrm{ft}^{3}$

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Step 2: Convert $\mathrm{ft}^{3}$ into gallons:
$? \mathrm{gal}=7.48 \mathrm{gal} \quad X 5 \underline{562} \mathrm{ft}^{3}=\underline{42,277}$ gallons (rounded)
4. What is the volume in gallons of a clear well that is 40 feet 8 inches square, and filled to 12 feet deep?

Step 1: Convert inches to feet

$$
\begin{aligned}
& \text { ?ft }=1 \mathrm{ft} \quad \mathrm{X} \\
& 12 \text { inches }
\end{aligned} \quad 8 \text { inches }=\underline{0.67} \mathrm{ft}
$$

Step 2: Insert diameter (in ft) into volume formula and do the math.
$V=(\mathrm{L})(\mathrm{W})(\mathrm{D})=(40.67 \mathrm{ft})(40.67 \mathrm{ft})(12 \mathrm{ft})=\underline{19848.5} \mathrm{ft}^{3}$
Step 3: Convert ft3 into gallons:

5. What is the volume in $\mathrm{ft}^{3}$ of an elevated clear well that is 17.5 feet in diameter, and filled to 14 feet?

Volume $\left(\mathrm{ft}^{3}\right)(0.785)(\mathrm{D})^{2}(\mathrm{~h})=$
$V=(0.785)(17.5 \mathrm{ft})(17.5 \mathrm{ft})(14 \mathrm{ft})=\underline{3,366 \mathrm{ft}^{3}}$
6. What is the pressure (psi) at the bottom of an elevated tank filled to 60 feet of water?
$? \mathrm{psi}=\frac{1 \mathrm{psi}}{2.31 \mathrm{ft}} \times \underline{60 \#}=\underline{60 \mathrm{psi}} \underline{2.31}=\underline{26} \mathrm{psi}$
7. Convert $80^{\circ} \mathrm{F}$ to ${ }^{\circ} \mathrm{C}$.
${ }^{\circ} \mathrm{C}=\frac{{ }^{\circ} \mathrm{F}-32}{1.8}$
${ }^{\circ} \mathrm{C}=\frac{80^{\circ} \mathrm{F}-32}{1.8}=\frac{48}{1.8}=\underline{27^{\circ} \mathrm{C}}$ (rounded)

## Equation \#1: Solving for lbs/day using the Feed Rate Formula

?lbs = Flow (MGD) X Dose(mg/L) X (8.34) day

This feed rate formula is represented in the following diagram called the Davidson Pie which was created by Gerald Davidson, Manager, Clear Lake Oaks Water District, Clear Lake Oaks, CA.

## Davidson Pie



Key Acronyms: MG = million gallons or MGD = million gallons per day
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Practice Problem: If a water treatment plant is putting out 14 MGD, and dosing soda ash at the rate of 5 $\mathrm{mg} / \mathrm{l}$, how many pounds will they use every day?
?lbs $=\operatorname{Flow}(M G D) \times$ Dose( $\mathrm{mg} / \mathrm{L}) X(8.34)$ day
$? \frac{\mathrm{lbs}}{\mathrm{day}}=14 \times 5 \times 8.34=\underline{\mathbf{5 8 4}}$

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Practice Problem: If a water treatment plant is making 0.150 MGD , and the chlorine dose is $1.2 \mathrm{mg} / \mathrm{l}$, how many pounds of gas chlorine will they use?
$? \underline{\mathrm{lbs}}=\operatorname{Flow}(\mathrm{MGD}) \times \operatorname{Dose}(\mathrm{mg} / \mathrm{L}) \mathrm{X}(8.34)$
day
$? \underline{\text { lbs }}=(0.15)(1.2)(8.34)=\underline{1.5}$
day

## Converting from GPD to MGD before solving with the formula

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Practice Problem: If a water treatment plant is making water at the rate of 300,000 gallons per day, and the chlorine dose is $2.0 \mathrm{mg} / \mathrm{l}$, how many pounds of gas chlorine will they use daily?

Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.
$\frac{? M G}{\text { day }}=1 \frac{\text { MG }}{1,000,000 \text { gallons }} \frac{300,000 \text { gallons }}{\text { day }}=0.30$ MGD

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) $\times$ Dose( $\mathrm{mg} / \mathrm{L}) \times 8.34$
$0.30 \times 2.0 \times 8.34=\underline{5} \mathrm{lb} / \mathrm{day}$

## Converting from GPM to MGD before solving with the formula

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Practice Problem: A water treatment plant operates at the rate of 200 gallons per minute. They dose soda ash at $5 \mathrm{mg} / \mathrm{L}$. How many pounds of soda ash will they use in a day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.
$? \frac{\mathrm{MG}}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gatlons }} \quad 200 \underset{\text { gat }}{\text { minute }} \times 1440 \frac{\text { minutes }}{\text { day }}=\underline{0.288} \frac{\mathrm{MG}}{\text { day }}$
Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) $\times$ Dose( $\mathrm{mg} / \mathrm{L}$ ) $\times 8.34$
$0.288 \times 5 \times 8.34=12 \mathrm{lb} /$ day

## Equation \#2: Solving for Dose ( $\mathrm{mg} / \mathrm{L}$ ) using the Feed Rate Formula

An operator can also use the pie chart formula to calculate the dose if the known factors are the feed rate in pounds per day, and the flow rate.
? Dose ( $\mathrm{mg} / \mathrm{L}$ ) $=$ Feed Rate, (lbs/ day)
Flow(MGD)(8.34)


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Practice Problem: A water treatment plant produces 150,000 gallons of water every day. It uses an average of 2 pounds of permanganate for iron and manganese removal. What is the dose of the permanganate?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\quad$ Feed Rate, lbs/day (Flow, MGD)(8.34)

Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, } \mathrm{lbs} / \text { day }}{(\text { Flow, MGD)(8.34) }}=\frac{(2) \mathrm{lbs} / \text { day }}{(0.15)(8.34)}$

Step 3: Multiply $0.15 \times 8.34$ in the denominator $=1.25$ (basic math rule)
Step 4: Perform the DOSE division: $\underline{2}$ (numerator) $=$ 1.56 mg 1.25 (denominator) L

## Equation \#3: Solving for Flow (MGD) using the Feed Rate Formula

Lastly, the pie chart formula can be used to calculate the flow if the dose and feed rate in pounds per day are known factors.

Example Problem: A water treatment plant uses 14 pounds of chlorine gas to treat their water daily. The chlorine dose is $1.5 \mathrm{mg} / \mathrm{I}$. What is their flow rate in MGD?


Vertical Format: Flow, MGD = Feed Rate, Ibs/per day (Dose, mg/L)(8.34)

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Practice Problem: A water treatment plant uses 8 pounds of chlorine daily and the dose is $17 \mathrm{mg} / \mathrm{l}$. How many gallons are they producing?

Step 1: Set up the variables in vertical format and insert known values
? Flow $(M G D)=\frac{\text { Feed Rate, Ibs/day }}{(\text { Dose })(8.34)}=\frac{(8) \mathrm{lb} / \text { day }}{(\underline{17)(8.34)}}$
Step 2: Multiply $\underline{17} \times 8.34$ in the denominator $=\underline{141.78}$ (basic math rule)
Step 3: Perform the FLOW division: 8 (numerator) $=0.056425$ MGD
141.78 (denominator)

Unit Cancellation Steps to solve for gallons/day
$\frac{? \text { gallons }}{\text { day }}=\frac{1,000.000 \text { gallons }}{1 \mathrm{MG}} \times 0.056425 \frac{\mathrm{MG}}{\text { day }}=56,425 \frac{\text { gallons }}{\text { day }}$

## Quiz \# 2

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1. How many pounds per day will be required if the dose is $13 \mathrm{mg} / \mathrm{L}$, and the flow treated is 1 MGD?
?lbs = Flow(MGD) X Dose(mg/L) X (8.34) $=(1)(13)(8.34)=\underline{108} \underline{\mathrm{lbs}}$
day
2. How many pounds per day will be required if the dose is $13 \mathrm{mg} / \mathrm{l}$, and the flow is at the rate of 695 gpm ?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.
$? \frac{\mathrm{MG}}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gallons }} \quad 695 \underset{\text { minute }}{\text { gat }} \times 1440 \frac{\text { minutes }}{\text { day }}=\frac{1.0 \mathrm{MG}}{\text { day }}$
Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow $(M G D) \times$ Dose $(\mathrm{mg} / \mathrm{L}) \times 8.34$
$1.0 \times 13 \times 8.34=\underline{108} \mathrm{lb} / \mathrm{day}$

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3. How many pounds per day will be needed to dose 335,000 gallons of water at $4 \mathrm{mg} / \mathrm{L}$ ?

Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.
$\frac{? M G}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gallons }} \frac{335,000 \text { gallons }}{\text { day }}=0.335 \mathrm{MGD}$

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow $(M G D) \times$ Dose $(\mathrm{mg} / \mathrm{L}) \times 8.34$
$0.335 \times 4.0 \times 8.34=\underline{11} \mathrm{lb} /$ day
4. What is the dose if 2.5 MGD were treated with 31 pounds of chlorine?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\quad$ Feed Rate, lbs/day (Flow, MGD)(8.34)

Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, Ibs/day }}{\text { (Flow, MGD)(8.34) }}=\frac{(31) \text { lbs/day }}{(2.5)(8.34)}$
Step 3: Multiply $2.5 \times 8.34$ in the denominator $=20.85$ (basic math rule)
Step 4: Perform the DOSE division: $\frac{31 \text { (numerator) }}{20.85 \text { (denominator) }} \quad \frac{1.5}{\frac{\mathrm{mg}}{\mathrm{L}}}$ (rounded)
5. How many pounds will be required if the flow is 95 gpm , and the dose is $7 \mathrm{mg} / \mathrm{L}$, and the plant runs for 12 hours per day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.
$\begin{aligned} & \text { ? MG }=1 \\ & \text { day } \\ & 1,000,000 \text { gallons }\end{aligned} \quad 95 \underline{\text { gal }} \times 60 \frac{\text { minutes }}{\text { minute }} \times 12 \frac{\mathrm{hrs}}{\text { day }}=0.0684 \frac{\mathrm{MG}}{\text { day }}$ for 12 hrs

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) $\times$ Dose(mg/L) $\times 8.34$
$0.0684 \times 7 \times 8.34=\underline{4} \mathrm{lb} /$ day (rounded)

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## Practice problems:

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1. How many pounds per day will be used when the dose is $5 \mathrm{mg} / \mathrm{L}$, and the flow rate is 350 gpm?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$
? \frac{\mathrm{MG}}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gallons }} 35 \underset{\text { minute }}{\text { gat }} \times 1440 \frac{\text { minutes }}{\text { day }}=0.5 \frac{\mathrm{MG}}{\text { day }}
$$

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) x Dose(mg/L) x 8.34
$0.5 \times 5 \times 8.34=\underline{21} \mathrm{lb} /$ day (rounded)
2. How many pounds per day will be needed if the flow rate is $80,000 \mathrm{gpd}$, and the dose is 25 $\mathrm{mg} / \mathrm{L}$ ?
Step 1: Convert gallons per day into million gallons per day (MGD) using unit cancellation.
$\frac{\mathrm{MG}}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gallons }} \frac{80,000 \text { gallons }}{\text { day }}=0.08 \mathrm{MGD}$

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) $\times$ Dose $(\mathrm{mg} / \mathrm{L}) \times 8.34$
$0.08 \times 25 \times 8.34=17 \mathrm{lb} /$ day
3. How many pounds per day will be used if the flow rate is 47 gpm through each filter, and there are 2 filters, and the dose is $7 \mathrm{mg} / \mathrm{L}$ ?

Step 1: Determine total flow rate for both filters by multiplying by 2
$47 \times 2=94 \mathrm{gpm}$
Step 2: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.

$$
? \frac{\mathrm{MG}}{\text { day }}=1 \frac{\mathrm{MG}}{1,000,000 \text { gallons }} \quad 94 \frac{\text { gat }}{\text { minute }} \times 1440 \frac{\text { minutes }}{\text { day }}=0.135 \frac{\mathrm{MG}}{\text { day }}
$$

Step 3: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow(MGD) $\times$ Dose $(\mathrm{mg} / \mathrm{L}) \times 8.34$
$0.135 \times 7 \times 8.34=\underline{8} \mathrm{lb} /$ day (rounded)
4. How many pounds per day will be used if the flow rate is 50 gpm , the dose is $4 \mathrm{mg} / \mathrm{L}$, and the plant operates for 16 hours each day?

Step 1: Convert gallons per minute into million gallons per day (MGD) using unit cancellation.
$? \underline{M G}=1 \mathrm{MG} \quad \times \quad 50$ gat $\times 60 \underline{\text { minutes }} \times 16 \underline{\mathrm{hrs}}=0.048 \underline{\mathrm{MG}}$ for 16 hrs day $1,000,000$ gallons minute hr day day

Step 2: Use MGD in feed rate formula to solve for Ibs/day
Feed Rate, lbs per day $=$ Flow $(M G D) \times$ Dose $(\mathrm{mg} / \mathrm{L}) \times 8.34$
$0.048 \times 4 \times 8.34=\underline{1.6} \mathrm{lb} / \mathrm{day}$
5. What is the dose if the total water treated is 650,000 gallons, and 22 pounds of chemical was used?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\quad$ Feed Rate, lbs/day (Flow, MGD)(8.34)

Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, lbs/day }}{(\text { Flow, MGD)(8.34) }}=\frac{(22) \text { lbs/day }}{(0.65)(8.34)}$

Step 3: Multiply $0.65 \times 8.34$ in the denominator $=20.85$ (basic math rule)

6. What is the dose if the plant uses 120 pounds of chemical each day to treat $1,350,000$ gallons daily?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, lbs/day }}{(\text { Flow, MGD)(8.34) }}$
Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, Ibs/day }}{(\text { Flow, MGD)(8.34) }}=\frac{(120) \mathrm{lbs} / \text { day }}{(1.35)(8.34)}$

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Step 3: Multiply $1.35 \times 8.34$ in the denominator $=11.25$ (basic math rule)
Step 4: Perform the DOSE division: $\frac{120 \text { (numerator) }}{11.25 \text { (denominator) }} \quad$ 11. $\frac{\mathrm{mg}}{\mathrm{L}}$ (rounded)
7. What is the dose if the operator uses 18 pounds of chemical to treat $650,000 \mathrm{gpd}$ ?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\quad$ Feed Rate, lbs/day
(Flow, MGD)(8.34)
Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, lbs/day }}{(\text { Flow, MGD)(8.34) }}=\frac{(18) \text { lbs/day }}{(0.65)(8.34)}$

Step 3: Multiply $0.65 \times 8.34$ in the denominator $=5.42$ (basic math rule)
Step 4: Perform the DOSE division: $\frac{18 \text { (numerator) }}{5.42 \text { (denominator) }} \quad \underline{3.3} \frac{\mathrm{mg}}{\mathrm{L}}$ (rounded)

## Feed Rate Calculations Using Flow with a \% Strength (i.e., \% pure) Solution

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Practice Problem: A water plant uses $15 \%$ sodium hypochlorite to disinfect the water. The dose is $1.2 \mathrm{mg} / \mathrm{L}$. They treat 0.25 million gallons per day. How many pounds of sodium hypochlorite will need to be fed?

Step 1: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? Pounds per day $=$ flow $x$ dose $\times 8.34=(0.25)(1.2)(8.34)=2.5$ pounds of chlorine is required.
Step 2: Calculate \# of pounds of $15 \%$ solution needed to achieve Step 1 feed rate.
a) Convert \% purity of solution into a decimal:
$15 \%=0.15$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the \% purity of the solution (as a decimal).
2.5 pounds $=16.7$ pounds of $15 \%$ hypochlorite.
0.15 (\% purity as a decimal)

TIP: Answer will always be more pounds than Step 1 result because solution is not 100\% pure.

Practice Problem: A water plant doses liquid alum at $5 \mathrm{mg} / \mathrm{L}$ and treats 1.5 MGD . How many pounds of liquid alum will be required daily to do this? Liquid alum is $481 / 2 \%$ pure.

Step 1: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? Pounds per day $=$ flow $x$ dose $\times 8.34=(1.5)(5)(8.34)=\underline{62.55}$ pound alum.
Step 2: Calculate \# of pounds of $15 \%$ solution needed to achieve Step 1 feed rate.
a) Convert \% purity of solution into a decimal:
$48.5 \%=\mathbf{0 . 4 8 5}$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the \% purity of the solution (as a decimal).
62.55 pounds $=\mathbf{1 2 8 . 9 6}$ or 129 pounds of liquid alum.
0.485 (\% purity as a decimal)

ANSWER KEY: 2019 Revised Basic Math

## Feed Rate Calculations Using Volume with a \% Strength (i.e., \% pure) Solution

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Practice Problem: Calculate the amount of calcium hypochlorite to dose a 500,000 gallon storage tank to a dose of $25 \mathrm{mg} / \mathrm{L}$ using granular calcium hypochlorite that indicates it is $65 \%$ chlorine.
Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.
?MG $=\frac{1 \mathrm{MG}}{1,000,000 \mathrm{gal}} \mathrm{X}(\underline{500,000}) \mathrm{gal}=\underline{\mathbf{0 . 5}} \mathrm{MG}$
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? lbs = volume $(\mathrm{MG}) \times$ dose $(\mathrm{mg} / \mathrm{L}) \times 8.34=(\underline{0.5})(\underline{25})(\underline{8.34})=\underline{104.25}$ pounds of chlorine is required.
Step 3: Calculate \# of pounds of $65 \%$ solution needed to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:
$\underline{65 \%}=\underline{0.65}$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the $\%$ purity of the solution (as a decimal).
104.25 pounds $=160.39$ pounds of $65 \%$ calcium hypochlorite. 0.65

## Calculating "Active Ingredient" Weight

Active ingredient weight is the number of pounds of "active ingredient" per gallon of a \% solution that cause a chemical reaction.

- This "active ingredient" weight value is then used in a calculation with the $100 \%$ pure "lbs/day" feed rate to determine the "gal/day" feed rate.

```
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    Calculating the Weight of the "Active ingredient" of a \% Solution Chemical
Practice Problem: How many pounds of caustic soda are there in a gallon of caustic soda that is
\(25 \%\) pure that has a specific gravity of 1.28 ?
Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical
Weight, lbs/gal = (Specific gravity of substance) \(x\) (weight of a gallon of water)
\(1.28 \times 8.34 \frac{\text { pounds }}{\text { gallon }}=\frac{10.67}{\frac{\text { pounds }}{\text { gallon }}}\)
Step 2: Determine the "active ingredient" weight of the caustic soda based on the \% purity
of solution
a) Convert \% purity of solution into a decimal:
\(25 \%=0.25\)
100\%
```


## b) Multiply the weight of a gallon (from step 1) by the \% purity of the product (as a decimal).

10.67 pounds $\times 0.25=\underline{\mathbf{2} .66}$ pounds of caustic soda in a gallon of $25 \%$ caustic soda solution gallon

This "active ingredient" weight provides the pounds of available caustic soda that is found in each gallon of $25 \%$ caustic soda solution. Within the 10.67 pounds of $25 \%$ caustic solution, there are 2.66 pounds of active ingredients.

## Using "Active Ingredient" Weight to Convert Feed Rate from Ibs/day to gal/day

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Practice Problem: A water plant uses sodium hypochlorite (12.5\%) to disinfect the water which provides $1.2 \mathrm{lbs} / \mathrm{gal}$ of available chlorine ("active ingredient" weight). The chlorine dosage is 1.6 $\mathrm{mg} / \mathrm{L}$. They treat 600,000 gallons per day. How many gallons of sodium hypochlorite will need to be fed?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.
? MGD $=\frac{1 \mathrm{MG}}{1,000,000 \text { gat }} X \frac{600,000 \text { (gal) }}{1 \text { day }}=\underline{0.6} \mathrm{MGD}$
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.6})(\underline{1.6})(8.34)=\underline{8}$ pounds of chlorine is required.
Step 3: Use "active ingredient" weight with unit cancellation steps to convert lbs/day to gal/day


NOTE: When you are given the "active ingredient" weight of a solution to solve a feed rate problem, you do not need to use the \% purity factor because it was used to derive the active ingredient weight.

ANSWER KEY: 2019 Revised Basic Math

## Quiz: 3

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1. How many pounds of alum ( $48.5 \%$ ) are required to treat 0.75 MGD with a dose of 12 $\mathrm{mg} / \mathrm{L}$ ?

Step 1: Solve for pounds (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.75})(\underline{12})(8.34)=\underline{75}$ pounds of chlorine is required.
Step 2: Calculate \# of pounds of $65 \%$ solution needed to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:
$48.5 \%=0.485$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the $\%$ purity of the solution (as a decimal).

75 pounds $=155$ pounds of $48.5 \%$ alum.
0.485 (\% purity as a decimal)
2. How many pounds of calcium hypochlorite (65 \%) are needed to treat 500,000 gallons per day with a dose of $2 \mathrm{mg} / \mathrm{L}$ ?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.
$? M G D=\frac{1 \mathrm{MG}}{1,000,000 \text { gal }} X \frac{500,000 \text { (gal) }}{1 \text { day }}=\underline{0.5}$ MGD
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.5})(\underline{2})(8.34)=\underline{8.34}$ pounds of chlorine is required.
Step 3: Calculate \# of pounds of \% solution needed (in this example, 65\%) to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:
$\underline{65 \%}=\underline{0.65}$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the \% purity of the solution (as a decimal).

0.65
3. How many pounds of sodium hypochlorite ( $121 / 2 \%$ ) are needed to treat a flow of 150 gallons per minute at a dose of $0.7 \mathrm{mg} / \mathrm{L}$ ?

Step 1: Convert flow in gallons (per minute) into MGD so that the feed rate (lbs/day) formula can be used.
?MGD $=\frac{1 \mathrm{MG}}{1,000,000 \text { gat }} \quad \times \frac{\text { volume of flow (gal) }}{1 \mathrm{~min}} \quad x \quad 1440 \frac{\mathrm{~min}}{\text { day }}$
$? \underline{M G}=1 \mathrm{MG} \quad x \quad 150$ gat $\times 1440$ minutes $=0.216 \underline{M G}$
day $1,000,000$ gallons minute day day
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.216})(\underline{0.7})(8.34)=\underline{1.26}$ pounds of chlorine is required.
Step 3: Calculate \# of pounds of $\%$ solution needed (in this example, $65 \%$ ) to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:
$\underline{12.5 \%}=0.125$
100\%
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the \% purity of the solution (as a decimal).
1.26 pounds $=10$ pounds of $12.5 \%$ sodium hypochlorite.
0.125

ANSWER KEY: 2019 Revised Basic Math
4. How many pounds of caustic soda are needed to dose water at $17 \mathrm{mg} / \mathrm{L}$ if you are treating $1,400,000$ gallons per day? The caustic soda concentration is 50 percent.

Step 1: Solve for pounds (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{1.4})(\underline{17})(8.34)=\underline{198}$ pounds of chlorine is required.

Step 2: Calculate \# of pounds of $65 \%$ solution needed to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:
$\frac{50 \%}{100 \%}=0.5$
b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the $\%$ purity of the solution (as a decimal).

198 pounds $=397$ pounds of $50 \%$ PAC
0.5 (\% purity as a decimal)
5. How many pounds of chlorine gas are required to treat 750,000 gallons of water to a dose of $50 \mathrm{mg} / \mathrm{L}$ for a 24 hour period?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.
? MGD $=\frac{1 \mathrm{MG}}{1,000,000 \text { gat }} \times \frac{750,000 \text { (gal) }}{1 \text { day }}=\underline{0.75} \mathrm{MGD}$
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.75})(\underline{50})(8.34)=\underline{313}$ pounds of chlorine is required.
6. A treatment plant uses $12.5 \%$ hypochlorite to disinfect the water. The required hypochlorite dosage is $2 \mathrm{mg} / \mathrm{L}$ and the plant flow is $300,000 \mathrm{gpd}$. How many gallons of $12.5 \%$ hypochlorite are required ( $12.5 \%$ hypo has $1.25 \mathrm{lbs} /$ gal available chlorine)?

Step 1: Convert flow in gallons (per day) into MGD so that the feed rate (lbs/day) formula can be used.
$? M G D=\frac{1 \mathrm{MG}}{1,000,000 \text { gat }} X \frac{300,000(\text { gal) }}{1 \text { day }}=0.3$ MGD

ANSWER KEY: 2019 Revised Basic Math

Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? pounds per day $=$ flow $x$ dose $\times 8.34=(\underline{0.3})(\underline{2})(8.34)=\underline{5}$ pounds of chlorine is required.
Step 3: Use "active ingredient" weight with unit cancellation steps to convert lbs/day to gal/day


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## Calculating the Weight of a Solution

Another consideration in water chemistry calculations is the weight of the product being used. For example, the weight of a gallon of water is 8.34 pounds. We learned earlier that there are 7.48 gallons in a cubic foot of water.

Practice Problem: What would be the weight of 100 gallons of water?
$? \mathrm{lbs}=8.34 \underline{\mathrm{lbs}} \times 100 \mathrm{gal}=834 \mathrm{lbs}$
gal

## Using Specific Gravity to calculate the weight of a solution

To calculate the weight of various chemicals we need to factor in the specific gravity of the chemical being used. Specific gravity is the weight of a substance compared to the weight of a gallon of water. Specific gravity information is found on the Safety Data Sheets (SDS) and is used to calculate the weight of a substance.

Total Weight, lbs/gal $=($ Specific gravity of substance) $\times$ (weight of a gallon of water)

Practice Problem: What is the weight of a gallon of sodium hypochlorite if the specific gravity is 1.11?

Weight, lbs/gal = (Specific gravity of substance) $x$ (weight of a gallon of water)

$$
? \mathrm{lbs}=1.11 \times 8.34 \mathrm{lbs}=9.26 \mathrm{lbs}
$$

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Practice Problem: What is the weight of a gallon of crankcase oil if the specific gravity is $0.89 ?$
Weight, lbs/gal = (Specific gravity of substance) $\times$ (weight of a gallon of water)
$? \frac{\mathrm{lbs}}{\mathrm{gal}}=0.89 \times 8.34 \frac{\mathrm{lbs}}{\mathrm{gal}}=7.4 \frac{\mathrm{lbs}}{\mathrm{gal}}$
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Calculating the weight of a drum

If you want to determine the weight of a drum or tank of solution, you must include that volume in your calculation.

$$
\text { Drum Weight, lbs }=(\text { gallons of drum or tank }) \times(\text { S.G. }) \times(8.34 \text { lbs/gal })
$$

Practice Problem: What would be the weight of a 50 gallon drum of $50 \%$ caustic soda if the specific gravity of the product is 1.53

Drum Weight, lbs $=($ gallons of drum or tank $) \times($ S.G. $) \times(8.34 \mathrm{lbs} / \mathrm{gal})$
? Drum weight, $\mathrm{lbs}=50 \times 1.53 \times 8.34=\underline{638} \mathrm{lbs}$.

## Calculating "Active Ingredient" Weight

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Practice Problem: What is the active ingredient weight of $48.5 \%$ alum that has a specific gravity of 1.33 .

## Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical

Weight, lbs/gal = (Specific gravity of substance) $\times$ (weight of a gallon of water)
$1.33 \times 8.34 \frac{\mathrm{lbs}}{\mathrm{gal}}=11.09 \frac{\mathrm{lbs}}{\mathrm{gal}}$
Step 2: Determine the "active ingredient" weight of the solution based on the \% purity of solution
a) Convert \% purity of solution into a decimal:
$48.5=0.485$

## ANSWER KEY: 2019 Revised Basic Math

100
b) Multiply the weight of a gallon (from step 1) by the \% purity of the product (as a decimal).
$11.09 \mathrm{lbs} \times 0.485=\mathbf{5 . 3 7}$ pounds of available alum in a gallon of $48.5 \%$ alum gal

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Calculating the active ingredient weight of a drum of solution

You can also calculate how many pounds of active ingredients there are in drum or tank of a liquid product.
? lbs of active ingredient within drum = drum volume (gal) x active ingredient weight (lbs/gal)

Example Problem: How many pounds of active ingredient are there in a 55 gallon drum of liquid alum if the product is $481 / 2$ percent pure with a specific gravity of 1.33 and the active ingredient weight is 5.37 lbs of alum/gal of product?
? Ibs of active ingredient within drum = active ingredient weight (lbs/gal) X drum volume (gal)
? lbs of active ingredient within drum $=5.37$ lbs $\times 55$ gat
gal
$=\underline{295.8} \mathrm{lbs}$ of active ingredient (alum) within the 48.5\%
solution

## Alternative Method of Calculating Active Ingredient Weight of a Drum:

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Example Problem: How many pounds of active ingredient are there in a 55 gallon drum of liquid alum if the product is $481 / 2$ percent pure with a specific gravity of 1.33 and the active ingredient weight is 5.37 lbs of alum/gal of product?

Step 1: Solve weight equation (lbs/gal) for the drum
Drum Weight, lbs $=($ gallons of drum or tank $) \times($ S.G. $) \times(8.34 \mathrm{lbs} /$ gal $)$
? Drum Weight, lbs $=55$ gal $\times 1.33 \times 8.34$

$$
=610 \mathrm{lbs}
$$

Step 2: Determine the "active ingredient" weight of the solution based on the \% purity of solution
a) Convert \% purity of solution into a decimal:
$\underline{48.5}=0.485$
100
b) Multiply the weight of the drum (from step 1) by the \% purity of the product (as a decimal).

610 lbs $\times 0.485=\underline{295.8} \mathrm{lbs}$ of active ingredient (alum) within the $48.5 \%$ alum solution

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## $\sqrt{ }$ Math Concept Exercise

1. In order to use the Feed Rate formula which is Ibs/day = Flow $x$ Dosage $\times 8.34$, name the units of measurement for the flow:
a) MGD
b) gpm
c) gpd
d) All of the above units can be used
2. If you have a flow in gpm, what calculation do you use to convert it to MGD?
a) Multiply gpm X 24 and divide by 1,000,000
b) Multiply gpm x 60 and divide by $1,000,000$
c) Multiply gpm $\times 1440$ and divide by $1,000,000$
d) Divide flow in gpm by $1,000,000$
3. If you have a flow in gpd, what calculation do you use to convert it to MGD?
a) Divide flow in gpd by 100
b) Divide flow in gpd by 10,000
c) Divide flow in gpd by 100,000
d) Divide flow in gpd by $1,000,000$
4. When using "active ingredient" weight to solve for "gallons", what calculation do you use?
a) ? gals = 1 gal $X$ "lbs" (as a \% solution feed rate) 1.63 lbs
b) ? gals = 1.63 lbs X "lbs" (as a \% solution feed rate)
gal

## Final Quiz :

1. What is the volume in gallons of a water tank that is 25 feet in diameter, and filled to a depth of 17 feet?

Step 1: Solve the volume equation in $\mathrm{ft}^{3}$ :
$\mathrm{V}=0.785(\mathrm{Dia})^{2}(\mathrm{H})$
$V=0.785(25 \mathrm{ft})(25 \mathrm{ft})(17 \mathrm{ft})=\underline{8340.6} \mathrm{ft}^{3}$
Step 2: Convert $\mathrm{ft}^{3}$ into gallons:
$?$ gal $=7.48 \underline{\mathrm{gal}} \quad X \underline{8340.6} \mathrm{ft}^{3}=\underline{62,388}$ gallons (rounded) $1 \mathrm{ft}^{3}$
2. What is the volume in gallons in a sedimentation basin that is 50 feet long, 35 feet wide, and filled to a depth of 12 feet?

Step 1: Solve the volume equation in $\mathrm{ft}^{3}$ :
$V=(L)(W)(H)$
$V=(50 \mathrm{ft})(35 \mathrm{ft})(12 \mathrm{ft})=\underline{\mathbf{2 1}, 000} \mathrm{ft}^{3}$
Step 2: Convert $\mathrm{ft}^{3}$ into gallons:

$$
? \mathrm{gal}=7.48 \mathrm{gal} \quad \times \underline{\mathbf{~ g a l}, 000} \mathrm{f}^{3}=\underline{157,080} \text { gallons (rounded) }
$$

## ANSWER KEY: 2019 Revised Basic Math

3. How many pounds of chemical will be fed if the dose required is $13 \mathrm{mg} / \mathrm{L}$, and the amount of water to be treated is 175,000 gallons per day?

Step 1: Convert flow (in gallons) into MG so that the feed rate (lbs) formula can be used.
?MG $=\frac{1 \mathrm{MG}}{1,000,000 \mathrm{gal}} \mathrm{X}(\underline{(175,000)}$ gal $=\underline{\mathbf{0 . 1 7 5}} \mathrm{MG}$
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? Ibs = volume $(\mathrm{MG}) \times$ dose $(\mathrm{mg} / \mathrm{L}) \times 8.34=(\underline{0.175})(\underline{13})(\underline{8.34})=\underline{19}$ pounds of chlorine is required. (rounded)
4. What is the dose if a water plant used 40 pounds of chemical, and treated 1.2 million gallons of water?

Step 1: Set up the variables in vertical format.
? Dose $(\mathrm{mg} / \mathrm{L})=\quad$ Feed Rate, lbs/day (Flow, MGD)(8.34)

Step 2: Insert known values into equation.
? Dose $(\mathrm{mg} / \mathrm{L})=\frac{\text { Feed Rate, lbs/day }}{(\text { Flow, MGD)(8.34) }}=\frac{(40) \text { lbs/day }}{(1.2)(8.34)}$

Step 3: Multiply $2.5 \times 8.34$ in the denominator $=10$ (basic math rule)
Step 4: Perform the DOSE division: $\frac{40 \text { (numerator) }}{10 \text { (denominator) }}=\quad 4 \frac{\mathrm{mg}}{\mathrm{L}}$
5. The target dose for a system is $1.2 \mathrm{mg} / \mathrm{L}$. They are treating an average of 300,000 gallons each day. How many lbs of sodium hypochlorite ( $121 / 2 \%$ ) will they need to feed?

Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.

$$
\text { ?MG }=\frac{1 \mathrm{MG}}{1,000,000 \mathrm{gal}} \mathrm{X}(\underline{(300,000)} \mathrm{gal}=\underline{0.3} \mathrm{MG}
$$

Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? Ibs = volume $(\mathrm{MG}) \times$ dose $(\mathrm{mg} / \mathrm{L}) \times 8.34=(\underline{0.3})(1.2)(\underline{8.34})=\underline{3}$ pounds of chlorine is required.
Step 3: Calculate \# of pounds of $65 \%$ solution needed to achieve Step 2 feed rate.
a) Convert \% purity of solution into a decimal:

## $\frac{12.5 \%}{100 \%}=\underline{0.125}$

b) Then divide the pounds needed (feed rate of $100 \%$ pure chemical) by the \% purity of the solution (as a decimal).

3 pounds $=\underline{24}$ pounds of $65 \%$ calcium hypochlorite.
0.125
6. The specific gravity of the hypochlorite is 1.11 . If the system needs to feed 24 pounds of hypochlorite, how many gallons will that require?

## Step 1: Solve weight equation (lbs/gal) for 1 gallon of chemical

Weight, lbs/gal = (Specific gravity of substance) $x$ (weight of a gallon of water)

$$
1.11 \times 8.34 \frac{\text { pounds }}{\text { gallon }}=9.26 \frac{\text { pounds }}{\text { gallon }}
$$

Step 2: Use weight of gallon of hypochlorite solution with unit cancellation steps to convert lbs/day to gal/day


## ANSWER KEY: 2019 Revised Basic Math

7. How many pounds of chlorine will be needed to disinfect a 250,000 gallon tank if a 50 $\mathrm{mg} / \mathrm{L}$ dose is required?

Step 1: Convert volume (in gallons) into MG so that the feed rate (lbs) formula can be used.
?MG $=\frac{1 \mathrm{MG}}{1,000,000 \mathrm{gal}} \underset{(\underline{250,000}) \mathrm{gal}=\underline{\mathbf{0 . 2 5}} \mathrm{MG}}{ }$
Step 2: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? $\mathrm{lbs}=$ volume $(\mathrm{MG}) \times$ dose $(\mathrm{mg} / \mathrm{L}) \times 8.34=(\underline{0.5})(\underline{25})(\underline{8.34})=\underline{104.25}$ pounds of chlorine is required.
8. What is the weight of the water that is in a container one foot long, one foot wide, and filled to a depth of 1 foot?

Step 1: Solve the volume equation in $\mathrm{ff}^{3}$ :
$\mathrm{V}=(\mathrm{L})(\mathrm{W})(\mathrm{H})$
$V=(1 \mathrm{ft})(1 \mathrm{ft})(1 \mathrm{ft})=\underline{1} \mathrm{ft}^{3}$
Step 2: Convert ft ${ }^{3}$ into gallons:
$? \mathrm{gal}=7.48 \mathrm{gal} \quad \mathrm{X} \underline{\mathrm{ft}^{3}} \quad=\underline{7.48}$ gallons
Step 3: Convert gallons into lbs.
$? \mathrm{lbs}=8.34 \underline{\mathrm{lbs}} \times 7.48 \mathrm{gat}=\underline{62.4} \mathrm{lbs}$
gal

9 How many pounds of aluminum sulfate (48.5\%) are required to dose water at $21 \mathrm{mg} / \mathrm{L}$ if the amount of water treated is 2 MGD?

Step 1: Solve for pounds per day (feed rate) for $100 \%$ pure chemical (no impurities).
? Pounds per day $=$ flow $x$ dose $\times 8.34=(2)(21)(8.34)=350.28$ pound alum.
Step 2: Calculate \# of pounds of $48.5 \%$ solution needed to achieve Step 1 feed rate.
a) Convert \% purity of solution into a decimal:
$\underline{48.5 \%}=\underline{0.485}$
100\%
b) Then divide the pounds needed (feed rate of 100\% pure chemical) by the \% purity of the solution (as a decimal).
350.28 pounds $=\underline{\mathbf{7 2 2}}$ pounds of liquid alum.
0.485 (\% purity as a decimal)
10. Convert a flow of 65 gallons per minute to the MGD unit.
?MGD $=\frac{1 \text { MG }}{1,000,000 \mathrm{gal}} \quad \times \frac{\text { volume of flow (gal) }}{1 \mathrm{~min}} \times 1440 \frac{\mathrm{~min}}{\text { day }}$
$? \underline{M G}=1 \mathrm{MG} \quad x \quad 65$ gat $\times 1440 \underline{\text { minutes }}=0.0936 \underline{M G}$
day 1,000,000 gallons minute
day day
11. How high (in ft) is the water column if the pressure at the bottom measures 40 psi ?
$? \mathrm{ft}=\frac{2.31 \mathrm{ft}}{1 \mathrm{psi}} \times 40 \mathrm{psi}=\underline{92} \mathrm{ft}$
12. Convert $17^{\circ} \mathrm{C}$ to ${ }^{\circ} \mathrm{F}$.
${ }^{\circ} \mathrm{F}=\left({ }^{\circ} \mathrm{C} \times 1.8\right)+32$
${ }^{\circ} \mathrm{F}=(17 \mathrm{X} 1.8)=31+32=\underline{63}{ }^{\circ} \mathrm{F}$
13. What is the \% unaccounted water if a system records the following readings:

The master meter reading is $1,500,000$ gallons.
The meter reading total is 965,000 gallons
Another 100,000 gallons were used for flushing, and 35,000 gallons were metered at a blow-off.

Step 1: Add total gallons accounted for (billed, blow-off, and flushing)
Gallons Accounted for $=\underline{965,000}$ (billed) $+\underline{\mathbf{3 5 , 0 0 0}}$ (blow-off) $+\underline{100,000}$ (flushing) $=\underline{1,100,000}$
Step 2: Subtract "accounted for" from total produced to find "Unaccounted for"
$1,500,000-1,100,000($ Step 1 Accounted for) $=\underline{400,000}$ (Unaccounted for)
Step 3: Divide "Unaccounted for" by total produced and multiply by 100 to equal the \% unaccounted for
$\underline{400,000}$ (Step 2 Unaccounted For) $=\underline{\mathbf{0 . 2 6 6}} \times 100=\underline{27} \%$ Unaccounted for (rounded) 1,500,000 (Total Produced)

